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COANDA-FLOW CLASSIFICATION OF TiO_2

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ABSTRACT

Coanda-flow classification has been shown to effectively handle TiO_2 . Present applications include removal of TiO_2 scrub solids grit and fine-cut (1-3 μm) separations. Potential energy benefits (primarily micronizer steam savings) from such classifications are now being studied. Removal of 7-8 wt. % + 325 mesh grit has already been shown to significantly reduce grinding energy requirements. Fine-cut separations are still being evaluated. In conjunction with the experimental program, a mathematical model of the Coanda-flow separation technique was formulated. The resulting cut-size predictions were in good agreement with the experimental results. This mathematical model was further used to analyze larger slot dimensions, etc. which would be more amenable to plant-scale operation.

COANDA-FLOW CLASSIFICATION OF TiO_2

INTRODUCTION

Size classification of TiO_2 is being investigated as a means of reducing energy consumption in the micronizer. The micronizer is the primary energy consumer in the plant, using $\sim 1/3$ of the total energy, and the particle size distribution of its feed is thought to affect its grinding efficiency. In particular, the presence of 5 to 10 wt. % scrub solids grit (+325 mesh) has been shown to significantly increase the micronizer steam consumption. In the present program Coanda-flow classification has been studied and shown to be effective in removing such grit. This same Coanda-flow technique is also being used to make fine-cut classifications. If the micronizer feed can be separated into two fractions, one of which is very fine, these two fractions could be micronized separately and thus avoid any overgrinding of the fines. Since TiO_2 is particularly sticky and hard to handle, past classification techniques have had difficulty with TiO_2 , and none have been able to make a fine enough cut-size to accomplish the above goal. The present technique shows the greatest promise for success. It has been shown to handle TiO_2 well and to make a cut as low as 2-3 μm .

OBJECTIVES

- Assess the feasibility of classifying TiO_2 in a Coanda-flow classifier.
- Determine the micronizer energy usage and pigment quality resulting from such size classification.

PATENT SITUATION

Patent Protection: None

Filing Action: None contemplated.

PROGRAM

A laboratory model based on Coanda-Flow principle is being constructed at the Engg. Test Center. Experimentation is planned for this Boundary-Layer classifier to determine what if any flow-balance problems may occur with the exit streams and to determine potential energy savings.

PUBLICATION STATUS

No plans for paper(s) at this time.

SPECIAL SAFETY PRECAUTIONS

Ear protection necessary.

ENVIRONMENTAL CONSIDERATIONS

None.

ACKNOWLEDGEMENTS

George Schurr had the original idea of using the Coanda-flow principle for scrub solids classification and has actively participated in the experimental programs discussed in this report. Phil Muhlmichl is responsible for the design of the laboratory apparatus. Professor Löffler and K. Mali (University of Karlsruhe, West Germany) are responsible for running our TiO_2 samples on their Uternal Jet classifier.

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SUMMARY AND CONCLUSIONS

The initial stage of this study included the design, construction, and testing of a laboratory Coanda-flow classifier for separating out TiO_2 scrub solids grit. (In the plant TiO_2 scrub solids, when used, constitute 4 to 8 wt. % of the TiO_2 .) This technique was shown to be an effective way to make such a separation and the resulting decrease in grinding energy usage was significant. In conjunction with the laboratory experiments, this classification technique was analyzed theoretically. Particle trajectories were mathematically modeled. By comparing the trajectories for different-sized particles, it was possible to predict the separation for different classifier conditions. The results were in good agreement with the experimental results, indicating that the model could be used to predict cut sizes under scaled-up conditions.

In the second part of this study fine-cut classifications were made on micronizer feed. A German Urtel Jet classifier (also based on the Coanda-flow principle) was used for these tests. The results were particularly good. The classifier effectively separated the TiO_2 and produced a very fine cut size (2-3 μm diameter top size). This is in agreement with the theoretical predictions. The investigation of energy usage and pigment quality is not completed yet, but some of the unm micronized fine fractions behaved very closely to standard grade pigments.

Plant-scale implementation has also been considered. Potential problem areas were identified and some of them were considered in detail. In particular, dimension changes were evaluated theoretically to determine whether the desired separations could still be made. The results suggest that such plant-scale separations are possible.

DISCUSSION

I. Description of Coanda-flow Separation Principle

Coanda flow occurs when a high velocity stream attaches itself to a solid and flows along the surface. In such case, the surface may be curved, irregular, etc., and the stream will deflect and follow the surface curvature rather than continue in a straight pathway. This principle can easily be adapted to produce a particle-size separation by using a convexly-curved surface, the resulting centrifugal force throwing the larger particles away from the surface while the fine particles are carried with the gas stream (Figure LSW-1)

II. Classifier Design

A. TiO₂ Scrub Solids Classification

To separate out TiO₂ scrub solids grit, a laboratory classifier based on the Coanda flow principle was designed and constructed (Figure LSW-2). To aid in the design, a theoretical analysis was made of the behavior of various size particles subjected to different gas velocities and radii of curvature. (This will be discussed in a later section.) The results of this analysis were used in selecting the dimensions for the laboratory model. They include: slot = 1/8" x 4"; radius of curvature = 4"; wedge + 3" from surface and displaced 60° from start of curvature. The fine fraction was collected by means of a bag filter while the coarse fraction was either collected by cyclone or allowed to fall by gravitation into a cotton bag. Both of these methods were satisfactory.

The ideal location for such a classifier in the plant would be at the end of the flue legs (i.e. after the pigment has been formed and cooled, and after the scrub solids have served their purpose of keeping the pipe walls clean and free of sticky pigment). At this point the pigment is dispersed in chlorine gas and is traveling at a velocity of ~100 ft/sec. The gas (air) used in the laboratory experiments differs only slightly in physical properties from the higher temperature (~150°C) chlorine in the flues. Also the air velocity used in the experiments (at the slot exit) was ~100 ft/sec to match that in the flues.

B. Classification of Micronizer Feed

To make a fine cut on micronizer feed, a German-made Urtel-Jet classifier was used. This required shipping the pigment samples to the University of Karlsruhe for the tests. George Schurr (ESD) observed some of these tests, and returned with a diagram of the classifier (Figure LSW-3). This classifier is also based on the Coanda-flow principle but has some slight differences (as compared to the scrub solids classifier) which give more control over the boundary layer flow of the gas. Thus it can produce a

finer separation. The velocity was 100 m/sec and the radius of curvature was 3/4". Also, a secondary gas stream flows at the same velocity as the pigment/gas mixture, and a curved section confines this stream as it flows ~30 to 40° around the Coanda surface. Thus a high velocity is maintained (i.e., the gas stream is not allowed to expand) while much of the pigment separation is occurring. Some expansion of the gas occurs as it proceeds farther around the Coanda surface, but surface suction is used to help keep the stream attached.

III. Theoretical Analysis

To predict cut size for a Coanda-flow classifier, a mathematical model was developed to compute particle trajectories for different-sized particles. For each individual particle a force balance was made. Since the particle is generally traveling in a direction different from the surrounding gas stream, the particle velocity was broken down into components - one in the direction of the gas flow; the other perpendicular to it. The gas velocity in this perpendicular direction was assumed to be zero.

Force Balances:

In the direction of gas flow:

drag force = acceleration

$$1/2 \rho_p \pi r^2 (v_g - v_{pg})^2 C_D = +(4/3) \pi r^3 \rho_p \left(\frac{dv_{pg}}{dt} \right)$$

In perpendicular direction:

drag force = deceleration

$$1/2 \rho_p \pi r^2 (v_{pp})^2 C_D = -(4/3) \pi r^3 \rho_p \left(\frac{dv_{pp}}{dt} \right)$$

where r = particle radius (cm)

ρ_p = particle density (gm/cm³)

v_{pg} = particle velocity in direction of gas flow (cm/sec)

ρ_g = gas density (gm/cm³)

v_{pp} = particle velocity in direction perpendicular to gas flow (cm/sec)

C_D = drag coefficient

v_g = gas velocity (cm/sec)

(Note: All particles are assumed spherical and gravity has been neglected.)

If the particle is large and manages to escape the flowing gas stream, the force balance reduces to a single expression for the direction of particle travel.

Drag Force = deceleration

$$\frac{1}{2} \rho_p \pi r^2 (v_p)^2 C_D = -(4/3) \pi r^3 \rho_p \left(\frac{dv_p}{dt} \right)$$

Where v_p = particle velocity (cm/sec)

The drag coefficient, and more importantly its functionality, vary with Reynolds number ($Re = 2\rho_g v r / \mu_g$ and v = particle velocity, μ_g = gas viscosity). However, the Reynolds number can be broken down into several ranges for which the resulting functionalities are all fairly simple (the commonly known relation for Stokes drag is $C_D = 24/Re$).

However, solution of these two force balances is complicated by the constantly changing direction of movement (and consequently the direction of the forces). Solution must therefore be done in small incremental time steps. At each time step, the differential equations can be solved analytically. The particle is then assumed to travel $v\Delta t$ in the appropriate direction and the procedure is repeated. A computer program was written to perform these calculations and to plot the resulting particle trajectories (Appendix).

Knowledge of the gas velocity profile is also necessary for this analysis. For the initial calculations (for the scrub solids classifier) a gradually expanding box-like profile was assumed (Figure LSW-4). No boundary layer (i.e., velocity dropping to zero) at the Coanda surface was included, as it was assumed to be so small that it would not play a role in the separation. Estimation of the boundary layer thickness based on boundary layer theory (Schlichting, 1968, p.26) confirms this. The calculated value at 1 cm from the slot exit is $\sim 10^{-5}$ cm, i.e., less than the diameter of a particle.

Actual velocity profiles were measured using a pitot tube and are shown in Figure LSW-5. The minimum distance from the surface at which a measurement could be made was 1/16". The surface boundary layer thickness was always less than 1/16", and therefore was never actually measured. Thus, the boundary layer as shown is not intended to be accurate in its indicated thickness, but rather to emphasize that such a boundary layer does exist.

These measured profiles are similar to those reported in the literature, but such profiles were not used in the theoretical calculations because they were too complex, and no correlation based on the slot exit velocity was available. More important, however, was the fact that the measured expansion rate of the gas stream was in fair agreement with the assumed rate, as this rate may affect the sharpness of the cut as well as the cut size.

The results of this mathematical analysis for a set of conditions similar to those in the flues (i.e., chlorine gas @ 150 C with a gas exit velocity of 100 ft/sec) and a Coanda surface radius of curvature of 10 cm with a 1/8" slot width are shown in Figure LSW-6.

These calculated trajectories indicate that the small particles (<10 μ m diameter) follow the gas stream around the Coanda surface. Slightly larger particles (10 to 50 μ m) have sufficient inertia to escape the flowing gas stream, but are then decelerated by the surrounding quiescent gas. The trajectory end points shown do indeed represent stopping points, but once the particle slows down (or stops), gravity will soon take over, causing it to fall back into the gas stream, and likely continue to move with the edge of this stream. The larger particles (> 50 μ m) escape the gas stream immediately and continue for long distances (>10") before gravity has any effect.

The easiest way to separate the grit will therefore be to place the separating wedge so that all of the gas flows along with the fine fraction. The expected cut size will then be ~50 μ m. Based on this information the laboratory scrub solids classifier was set up with the wedge about 3" from the surface at ~60° around. A typical experimental run gave the following results

Wet screen analysis of feed

+80 mesh	6.53 wt.%
-80 +325 mesh	1.32 wt.%

Classified - Fine fraction

+80 mesh	0.30 wt.%
-80 +325 mesh	0.42 wt.%

This indicates that the cut was near 325 mesh as predicted. (Although it appears that only ~2/3 of the 80 to 325 mesh was classified out, the actual value is probably higher (possibly as high as 80%). This is due to a small loss of fines when running small samples in the present system.

The accuracy of the mathematical model was further demonstrated when it was used to predict the cut size for the Uternal Jet classifier. (A non-expanding gas profile was assumed for these calculations.) In this case the separating wedge actually splits the gas flow, and the sharpness of the cut will depend more strongly on the height of the slot. For instance, if a sharp cut between 2 and 3 μ m is desired, a 3 μ m particle exiting next to the surface (Fig. LSW-7) must be separable from a 2 μ m particle exiting from the top of the

slot (Fig. LSW-8). Based on the particle trajectories a reasonable separation can be made as low as 1 to 2 μm , but a really sharp separation is probably possible only at $\sim 5 \mu\text{m}$. For the present location of the separator (1/4" from the surface and $\sim 120^\circ$ around), the predicted cut is between 1 and 2 μm with top size of $\sim 1.5 \mu\text{m}$, and indeed the resulting fine fraction had a top size of 2 to 3 μm . The coarse fraction, as expected, did contain some of the fine particles, but only a small percentage of the original sample.

EXPERIMENTATION

Samples of R900 and R960 dryer discharge (micronizer feed) were classified in the Coanda-flow scrub solids classifier. The "as is" R900 DD contained $\sim 8 \text{ wt.}\%$ +325 mesh grit. Almost all of this grit was in the size range 20 to 40 mesh. The R960 DD, on the other hand, contained $< 1 \text{ wt.}\%$ grit (apparently it had been produced using salt scrubs). For testing purposes $\sim 7 \text{ wt.}\%$ grit (20 to 40 mesh) was added to it. The Coanda classifier effectively separated out the grit in both of these samples. However, pigment stickiness and ease of deagglomeration are important. A sample of R101 containing 6 wt.% grit could not be classified well because much of the fine pigment remained agglomerated in the injector and thus behaved like grit during classification (i.e., much of the fine pigment was collected in the coarse fraction).

To determine grinding energy requirements, samples were classified and micronized at various steam/pigment levels in the Edge Moor 8" micronizer. They were then compared to unclassified samples similarly micronized. Since gloss is the property most strongly affected by the grinding energy level, all samples were analyzed for gloss in both alkyd and aqueous formulations. The results (Figs. LSW-9 and 10) show reduced grinding energy requirements for grit-free samples. The actual energy requirements of the large plant micronizers may, however, differ somewhat from those of the 8" experimental micronizer, but the present results do suggest that significant grinding energy reductions may be possible.

The purpose of classifying the micronizer feed (dryer discharge) with the Uternal Jet was to split it into two fractions which when micronized separately would require less grinding energy. This would occur if the present process overgrinds the fines or if a narrower particle size distribution is more efficiently ground. Samples of R900 and R931 DD were sent to Germany for classification in the Uternal Jet. Upon return, both coarse and fine fractions were micronized at various S/P levels and compared to unclassified samples similarly micronized. Analyses of the samples included particle size distribution for the original R900 DD and R931 DD and the classified samples. (Figures LSW 11 and 12) According to the sedigraph results the mass does not balance. At the present time we do not know why, but further study is planned once the Engineering Department completes their own boundary layer classifier. Paint formulations were used to determine gloss

for the R900 samples and hiding power for the R931 samples. The results are plotted in Fig. LSW-13. The most significant result was the high hiding power for the unmiconized R931 fine fraction - this sample was just below standard pigment quality in its behavior. Attempts to determine the grinding energy requirement for this fine fraction, however, have been inconclusive. The 8" micronizer could not be run at a S/P ratio low enough to distinguish between the classified and the unclassified (i.e., both samples had good hiding power at this lowest S/P). A low energy hammermill was subsequently tried, but its grinding energy level may have been too low as there was no improvement in the R931 fine fraction.

Problems were also encountered with the R900 samples. One of the R900 fine fractions had an impressively high gloss value, but was irreproducible - the initial measurement gave 77 and several repetitions gave 42. The micronization tests were again inconclusive. This particular sample of R900 micronizer feed was so good that even at the lowest S/P (on the 8" micronizer) a very high gloss pigment resulted. Thus differences in energy requirements between classified and unclassified pigment could not be determined. A further test was made using sandmilling, a lower energy type of grinding. The resulting slurries, however, produced very poor gritty paint films. (It is not certain whether the slurry preparation technique had any effect on this or whether it was solely due to poor pigment quality.) To resolve the question of energy usage, a poorer (more normal) quality R900 micronizer feed will be used in future tests.

To determine overall energy requirements, the coarse fractions must also be evaluated. Some micronization tests have already been done on the R900 coarse fraction. The results suggest that more grinding energy is required (as compared to an unclassified sample), but the observed gloss differences were within the accuracy limits of the measurement and thus inconclusive. The R931 coarse fraction has not been evaluated, as the original sample pelletized in transit to Germany. These pellets were removed before classification so it is uncertain whether the resulting coarse fraction (and possibly even the fine fraction) are representative of fresh plant samples. Further experimental work with fresh pigment is planned.

SCALE-UP CONSIDERATIONS

For scrub solids grit classification either the laboratory model or the Uternal Jet design could be used. However, the laboratory Coanda model would likely use the least amount of extra gas. If such a classifier is to be used at the end of the flues, the pigment would be in a chlorine atmosphere and additional gas would have to be chlorine as well. Thus large quantities may be undesirable. On the other hand, the controlled boundary layer flow of the Uternal Jet would undoubtedly insure a sharper cut at 325

mesh. The Uternal Jet could also be used to make a dual separation (grit elimination plus fine-cut classification) after the pigment has been collected in the cyclone. This would require an air stream to disperse the pigment, whereas for classification in the flues we would assume that the pigment is already dispersed (i.e., deagglomerated). However, logistically it may be difficult for the plant to handle two separate streams (the fine and coarse fractions) through the remainder of the process, i.e. wet treatment, filtration, drying, and micronization.

I. Scrub Solids Classification

For the present analysis we will first consider the laboratory Coanda design. For scrub solids classification at the end of the flues, the slot height must be large enough to avoid plugging. Also the JV plant cannot tolerate an in-line pressure drop; i.e. orifice flow must be avoided or additional blowers will be necessary to inject the pigment. Orifice flow can be avoided by maintaining the same cross-sectional area going from the flues into the slot. For example, the flues end with a 12" diameter pipe, thus having a cross-sectional area of 112 in². To maintain this area, a slot of height 1" would have to be 112" long. A more reasonable size would be either 2" x 56" or 3" x 37". Thus the major scale-up considerations (assuming gas velocity and pigment concentrations are kept the same) will be:

- 1) how large (height) a slot can be used without sacrificing cut sharpness.
- 2) how long will the stream stay attached to the Coanda surface if a large slot is used.
- 3) how much additional gas is needed for mixing as the boundary layer expands.

A correlation for detachment angle was given in the literature (B. G. Newman, 1961).

$$\theta_{\text{sep}} = 245 - \frac{391(b/a)}{1 + (9/8)(b/a)} \quad \text{(See Figure LSW-14 for Newman's Coanda configuration)}$$

where θ_{sep} = detachment angle (degrees); the angle refers to the angular displacement around the Coanda surface

b = slot height
a = radius of curvature

This expression, however, is only valid for Reynolds numbers (where Re is defined as $[(P - P_{\infty}) ba / \rho v^2]^{1/2}$) greater than some limiting value. Newman's experimental results gave a limiting value of $Re \approx 4 \times 10^4$, but the b/a values which he studied were quite low (0.0067 to 0.04). He further states, that the Re value should deviate less than 5% for b/a up to 1 and that the value (4×10^4) is not known to that accuracy. (His data suggest an accuracy of $\approx 10\%$.)

The following three cases (for the original Coanda-flow design) were selected to represent the range of practical plant-scale conditions:

- 1) 6 in. radius of curvature; 2" x 56" slot
- 2) 8 in. radius of curvature; 2" x 56" slot
- 3) 8 in. radius of curvature; 3" x 37" slot

To determine whether these conditions would still give the desired separation, the above correlation was used along with a computer analysis of the particle trajectories. The accuracy of Newman's correlation is not known for the desired range of $b/a \geq 0.25$ but Newman expects it to be reasonably accurate for $b/a \leq 1.0$. The expression was, therefore, used only to obtain an estimate. If the original scrub solids classifier design were used, we would need the gas stream to remain attached at least 90° . However, to obtain an estimate a value of 150° was used to include a margin of safety. This resulted in a b/a value of $\approx 1/3$.

As a check on the usefulness of the Newman expression the slot Reynolds number was calculated for the following conditions:

$$\begin{aligned} ab &= 12 (2 \times 6) \text{ in}^2 & \text{where } \rho &= 0.004 \text{ (Cl}_2 \text{ @ } 150^\circ\text{C)} \\ (P-p)_{\infty} &= \frac{1}{2} \rho v^2 & v &= 3000 \text{ cm/sec} \\ v &= \mu / \rho & \mu &= 0.0002 \text{ poise (Cl}_2 \text{ @ } 150^\circ\text{C)} \end{aligned}$$

The resulting value was 1.5×10^5 which is above the desired minimum.

Another consideration is the slot aspect ratio (length/height). In the literature, one study (McGlaughlin and Greber, 1967) was reported in which aspect ratios of 0.8 to 2.4 were used, and the gas streams detached much earlier than predicted by the above expression. Newman's experiments, on the other hand, were in the range of 200 to 1200. It is not known how large the aspect ratio must be to avoid problems, but probably 10 to 20 would be a good guess. In the laboratory scrub solids classifier, a value of ≈ 30 was used. In the Urtanal Jet the ratio was 11. In the three selected cases, the aspect ratio is ≥ 12 .

The computer results for the three cases are shown in Figs. LSW-15, 16 and 17. In general, the use of such large slot widths causes a considerable sacrifice in the sharpness of the cut, and the exact location of the separating wedge will be much more critical than it was in the laboratory model. This effect is shown quite clearly in Fig. LSW-18, which gives particle trajectories for particles exiting from different locations in the slot. If the separator is carefully placed, a separation at $\sim 40\mu\text{m}$ could be made. The cut would not be as sharp as in the lab model, but probably sharp enough. However, this requires the separator to be in the middle of the gas stream and would require gas flow balance and control on the exiting streams. If on the other hand, the separator is placed outside of the gas flow, all of the gas will be associated with the fine fraction and gas handling would be much easier. However, the cut size will be considerably greater, ranging from 70 to 150 μm . Of the three cases, the 2" slot with the 6" radius of curvature gives the finest cut. The case of the 8" radius of curvature with the 2" slot is similar to the previous case, but the gas flow is more expanded. This will cause an even greater loss in the cut sharpness and possibly some increase in cut size. The third case is the worst and would certainly not be recommended. In fact, in general, the smaller the slot height, the better will be the cut sharpness. Also, a smaller radius of curvature will be possible, which in turn will decrease the cut size. Based on this information, the first case (2" x 56" slot height, with 6" radius of curvature) would be recommended. An even smaller slot height, such as 1½" (length = 75") or 1-¾" (length = 65") would be better, if the slot length does not pose a problem in design and construction.

Another consideration for plant-scale feasibility is the amount of surrounding gas which becomes entrained in the pigment/gas jet as it flows around the Coanda surface. No exact correlation was available for the present configuration. However, Giles et al (1965) reported an approximate formula for a logarithmic spiral surface.

$$V_E = 1/2 U (Y_{m/2}/s)$$

where V_E = entrainment velocity

$$\text{or } \frac{(\text{vol. entrained})}{(\text{dist. traveled around surface})(\text{slot length})(\text{time})}$$

U = maximum velocity for any given distance around surface

$Y_{m/2}$ = half jet thickness (see Fig. LSW-8)

s = distance around surface (i.e., travel distance from slot exit)

This formula was used to obtain an order-of-magnitude estimate for the laboratory Coanda-flow classifier design. For a circular Coanda surface, $Y_m/2/s$ is not constant along the surface. Therefore, an average value was used, and based on the experimentally determined velocities, a value of 0.2 was selected. U also varies as the stream progresses. Again, an average value was used - in this case, one-half of the exit velocity. The resulting value of V_E was 150 cm/sec. For the previously-mentioned case of a 2" x 56" slot with a 6" radius of curvature, the gas flow rate through the slot would be $\approx 78 \text{ ft}^3/\text{sec}$, while the total entrainment would be $\approx 18 \text{ ft}^3/\text{sec}$ or $\approx 1/5$ of the jet flow rate. To avoid undue turbulence in the plant classifier, it may, therefore, be necessary to have a bleed stream of this magnitude situated above the slot.

If the Uternal Jet design were used for scrub solids classification at the end of the flues we would still want a large slot for the pigment feed. Thus we would probably want to change some of the other dimensions such as the radius of curvature. For instance, the radius of curvature could be 4", the pigment slot 1 1/2" and the additional gas slot 2 1/2". θ_{sep} for these conditions is $\sim 60^\circ$ (see next section on Uternal Jet fine cut classification for further explanation). The predicted cut size for this was $\sim 5\mu\text{m}$ (Figs. 19 & 20).

Regardless of the classifier design, the state of pigment agglomeration will be important. If the pigment is not well-dispersed at the end of the flues, a sharp separation cannot be obtained without supplying extra energy to break up the agglomerates. A separate study (W. E. Stevens) is already underway to determine the degree of dispersion at other points along the flues, and we have requested that he also include a measurement at the end. This information will then be used in our assessment of plant-scale feasibility.

II. Classification of Micronizer Feed

Scale-up of the Uternal Jet for use as a fine-cut classifier would primarily consist of making the total slot length great enough to handle the pigment rate in the plant. Otherwise, there would be no change in dimensions. Analysis of the design, however, did clarify the operation of such a classifier. The slot height (in Newman's expression) is actually the combined heights of the pigment feed slot and the additional air slot totalling ~ 1.25 in. Therefore

$$\begin{aligned}\theta_{\text{sep}} &= 245 - \frac{391(1.25/0.75)}{1 + (9/8)(1.25/0.75)} \\ &= 18.3^\circ\end{aligned}$$

(The "Re" was calculated for these conditions and is above the minimum value.)

This angular distance is quite small, but much of the separation is actually produced within the air slot (i.e., after the pigment exits but within the region of controlled flow). Also the suction on the Coanda surface may be very important in keeping the stream attached. A small pigment feed slot will be important to maintain good cut sharpness, but increasing it from 1/4" to 1/2" may be all right. Some idea of the required length can be determined from the experimental feed rates. If one production line makes 100,000 tons/yr. (10,300 kg/hr.) and the feed rate is twice the experimental (because the slot height has been doubled), - $2 \times 200 = 400$ kg/hr., the needed length is

$$\frac{10,300}{400} (8 \text{ cm}) = 206 \text{ cm.} = 82.5 \text{ in.}$$

This total length could be provided by using several classifiers; for instance 4 classifiers each having $\sqrt[3]{20}$ " long slot.

A possible disadvantage of this unit, however, is the need to balance the flows of exiting gas streams. It is not known how critical this will be, but further studies are planned to determine this.

Other Applications

The Coanda-flow classification principle can also be used to separate particles of different density.

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INDEXING TERMS

Boundary Layer Classifier
Classification
Coanda-flow
Titanium Dioxide
Uternal Jet

FIGURE LSW-1

COANDA CLASSIFIER

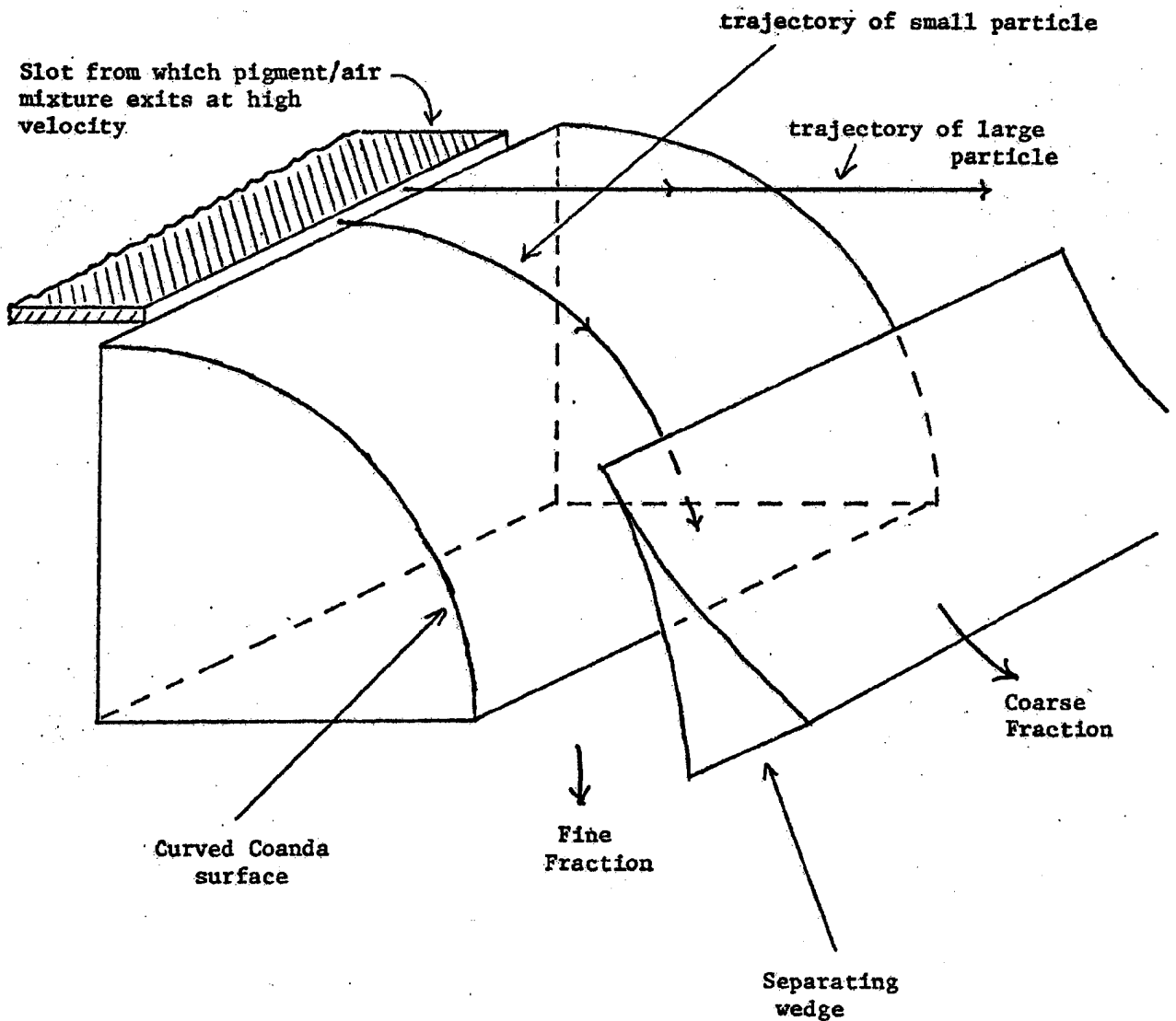


FIGURE LSW-2

LABORATORY APPARATUS

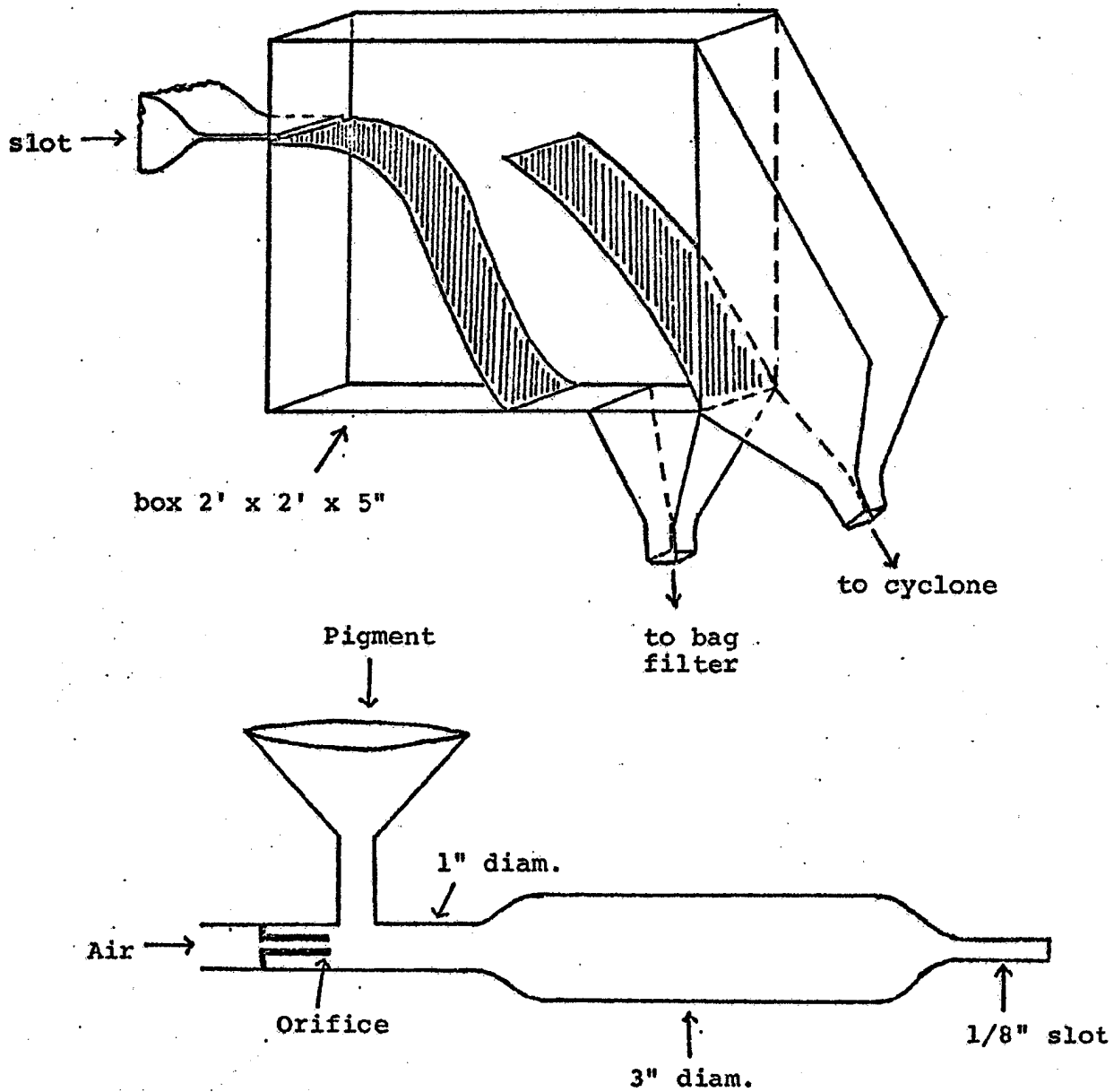


Figure LSW-3

INTERNAL CLASSIFIER

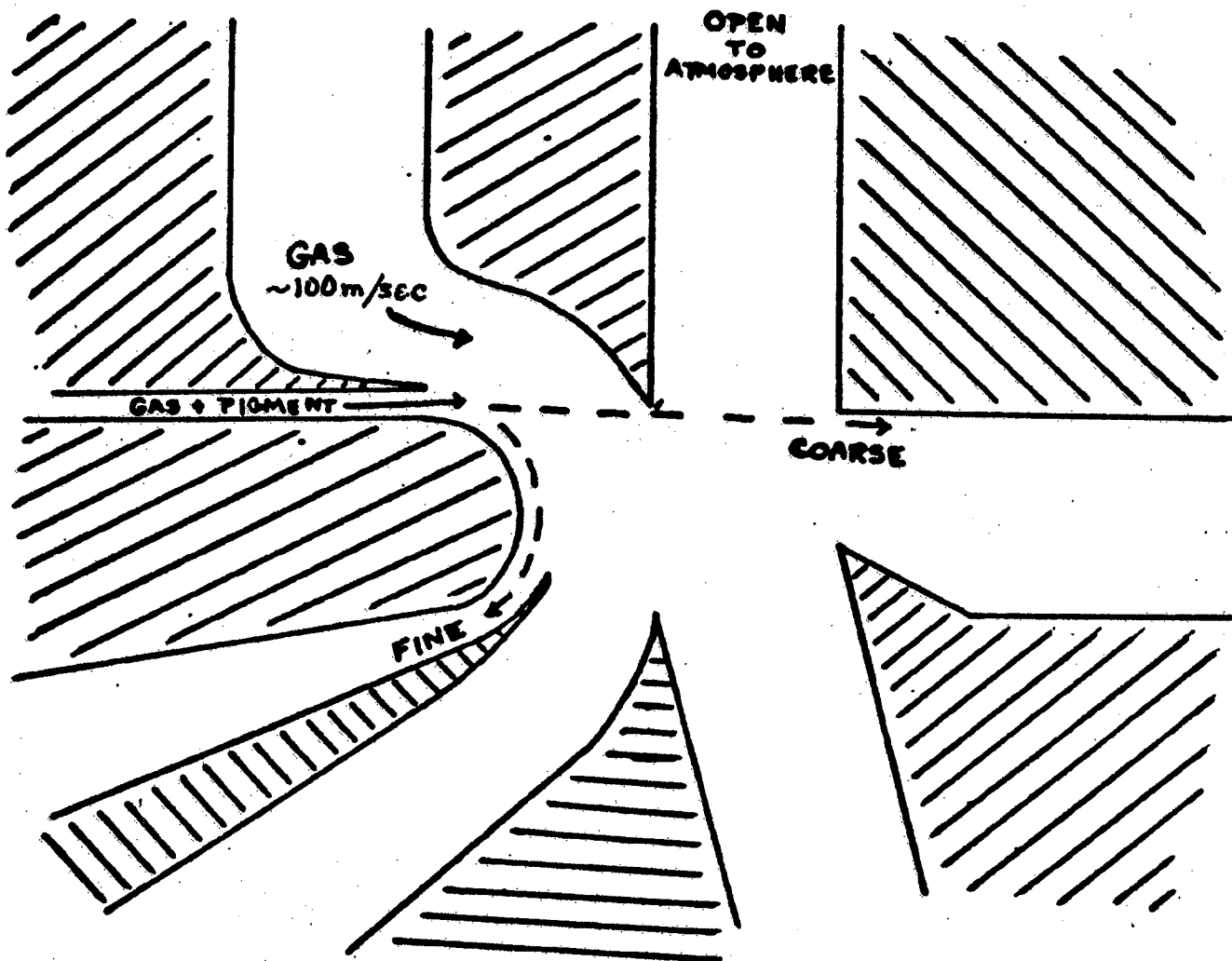
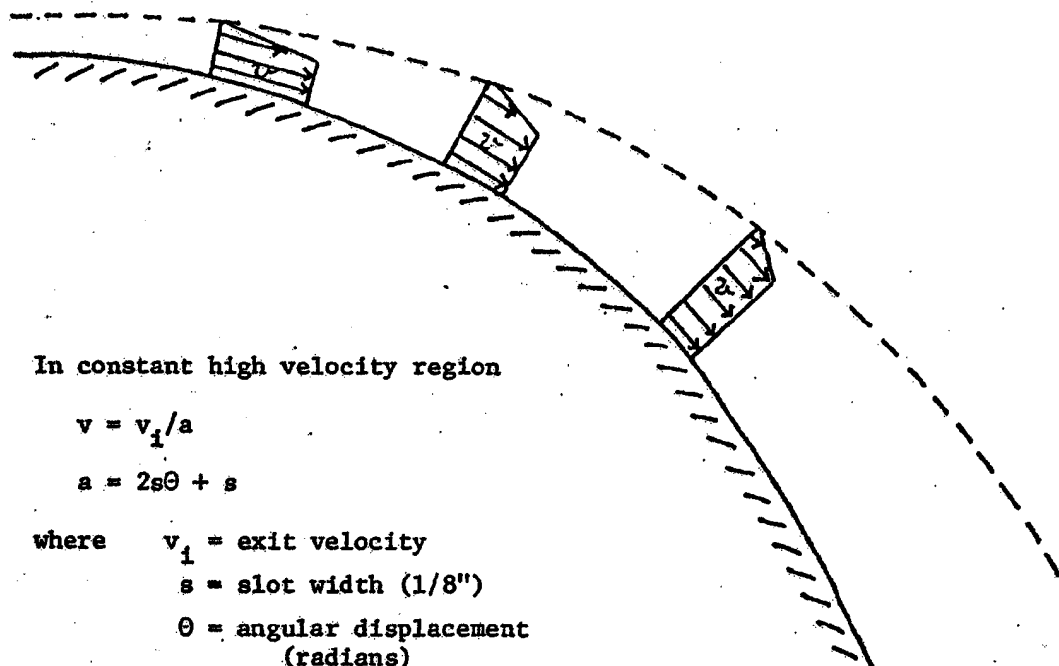


FIGURE LSW-4
ASSUMED GAS VELOCITY PROFILES



In constant high velocity region

$$v = v_1/a$$

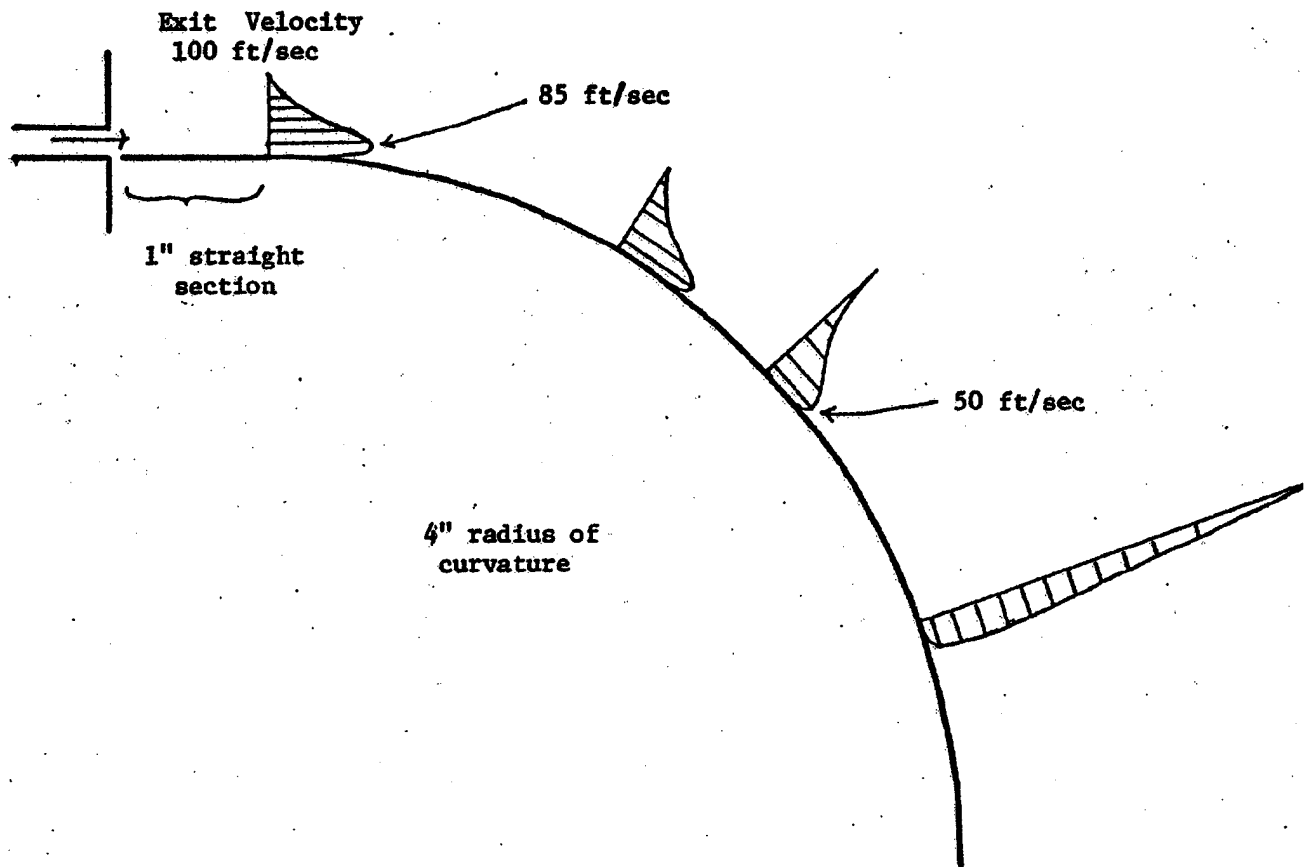
$$a = 2s\theta + s$$

where v_1 = exit velocity
 s = slot width (1/8")
 θ = angular displacement
(radians)

Note - No initial straight section was assumed, however the actual surface did include one (see Figure LSW-2). This figure is not drawn to scale.

FIGURE LSW-5

MEASURED VELOCITY PROFILES



(Drawn to scale)

Figure LSW-6
Particle Trajectories in a Coanda Classifier
4" Radius of Curvature

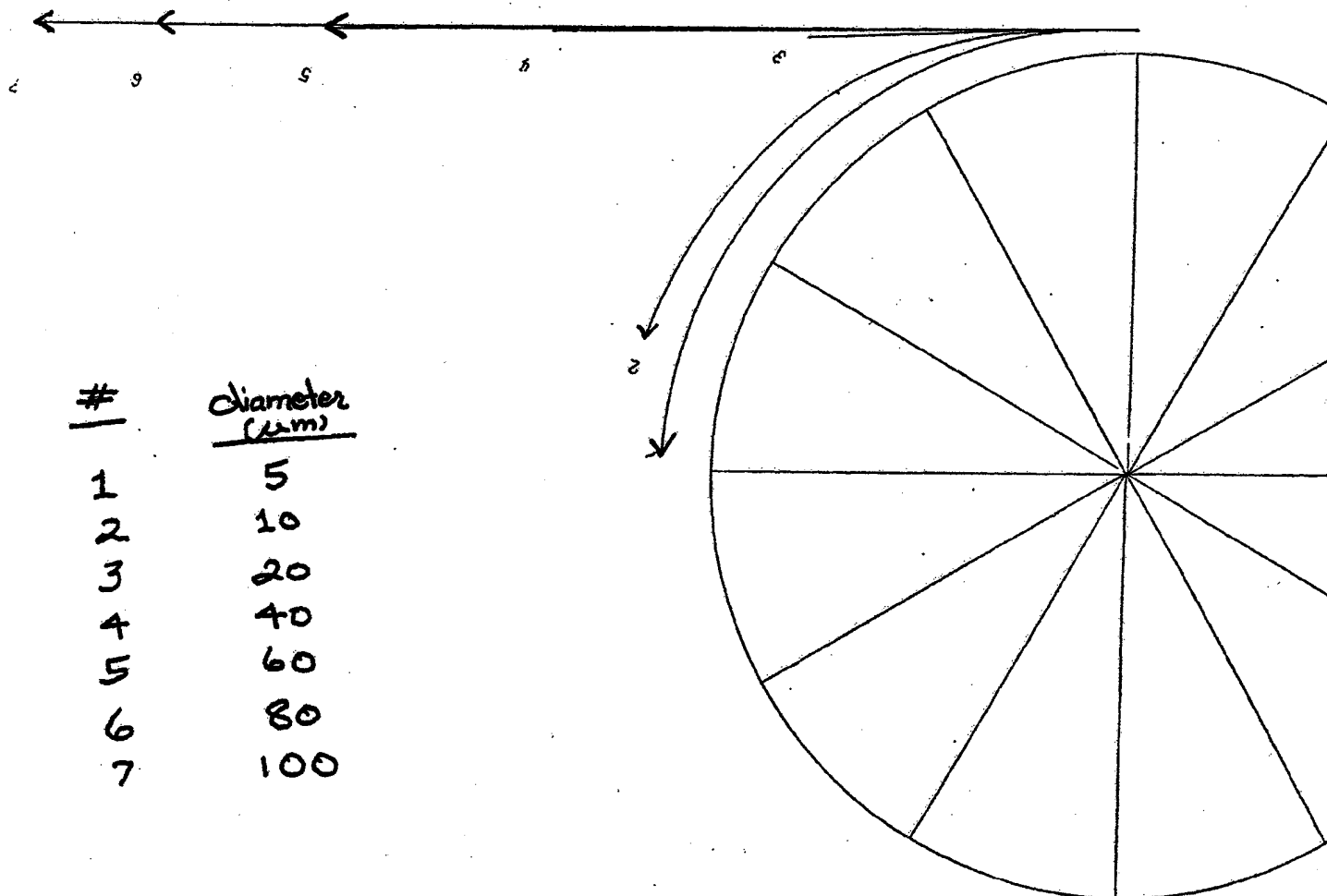


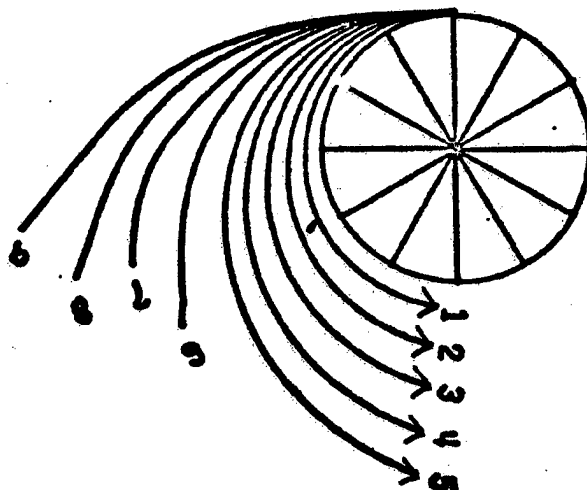
Figure LSW-7

PARTICLE TRAJECTORIES

CONDITIONS : AIR, Rm. Temp.

$V = 3000 \text{ CM/SEC}$,

PART. DENS = 4.0 g/CM^3



DIAMETERS

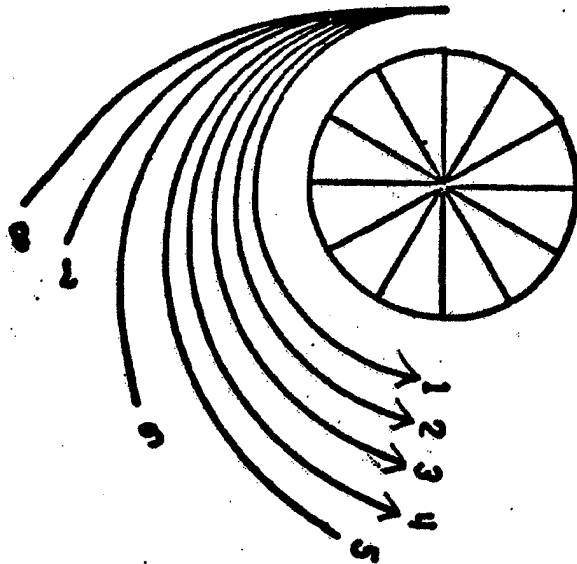
1 - $1 \mu\text{m}$
2 - $2 \mu\text{m}$
3 - $3 \mu\text{m}$
4 - $4 \mu\text{m}$
5 - $5 \mu\text{m}$

6 - $7 \mu\text{m}$
7 - $9 \mu\text{m}$
8 - $12 \mu\text{m}$
9 - $15 \mu\text{m}$

Figure LSW-8

PARTICLE TRAJECTORIES

(Same as Figure LSW-7
but Exiting from Top
of Slot)



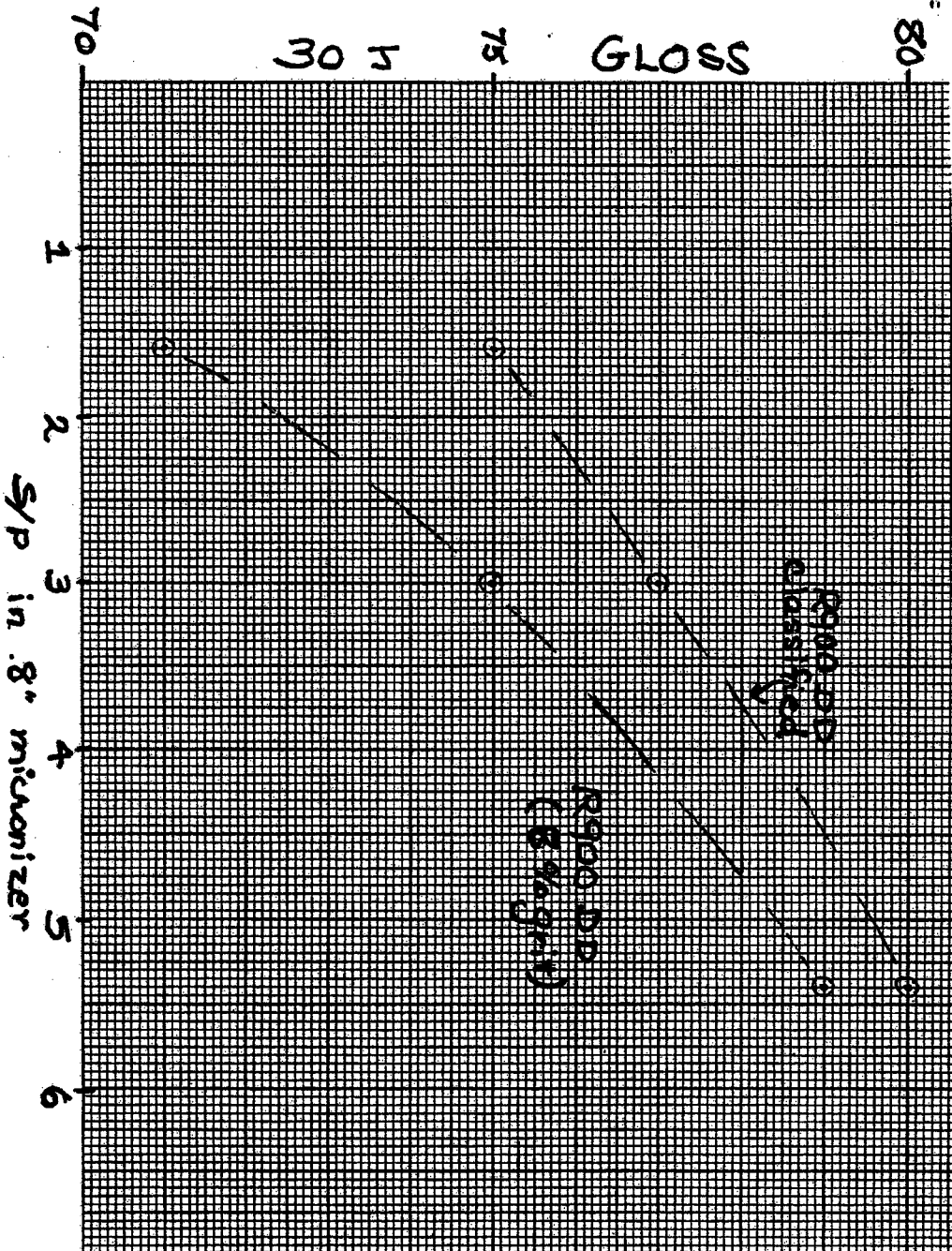


Figure LSW-10

EFFECT OF GRIT REMOVAL ON R960

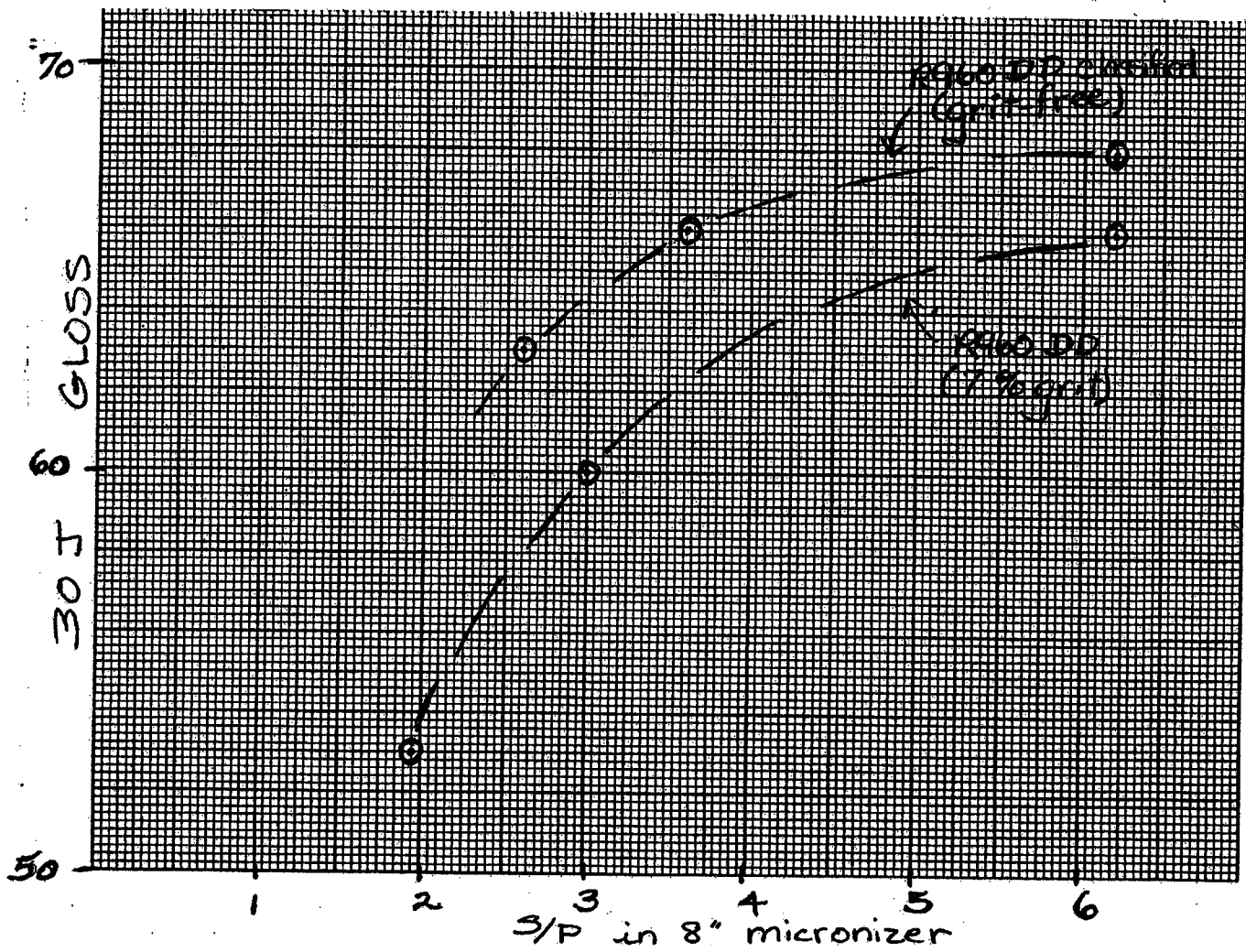
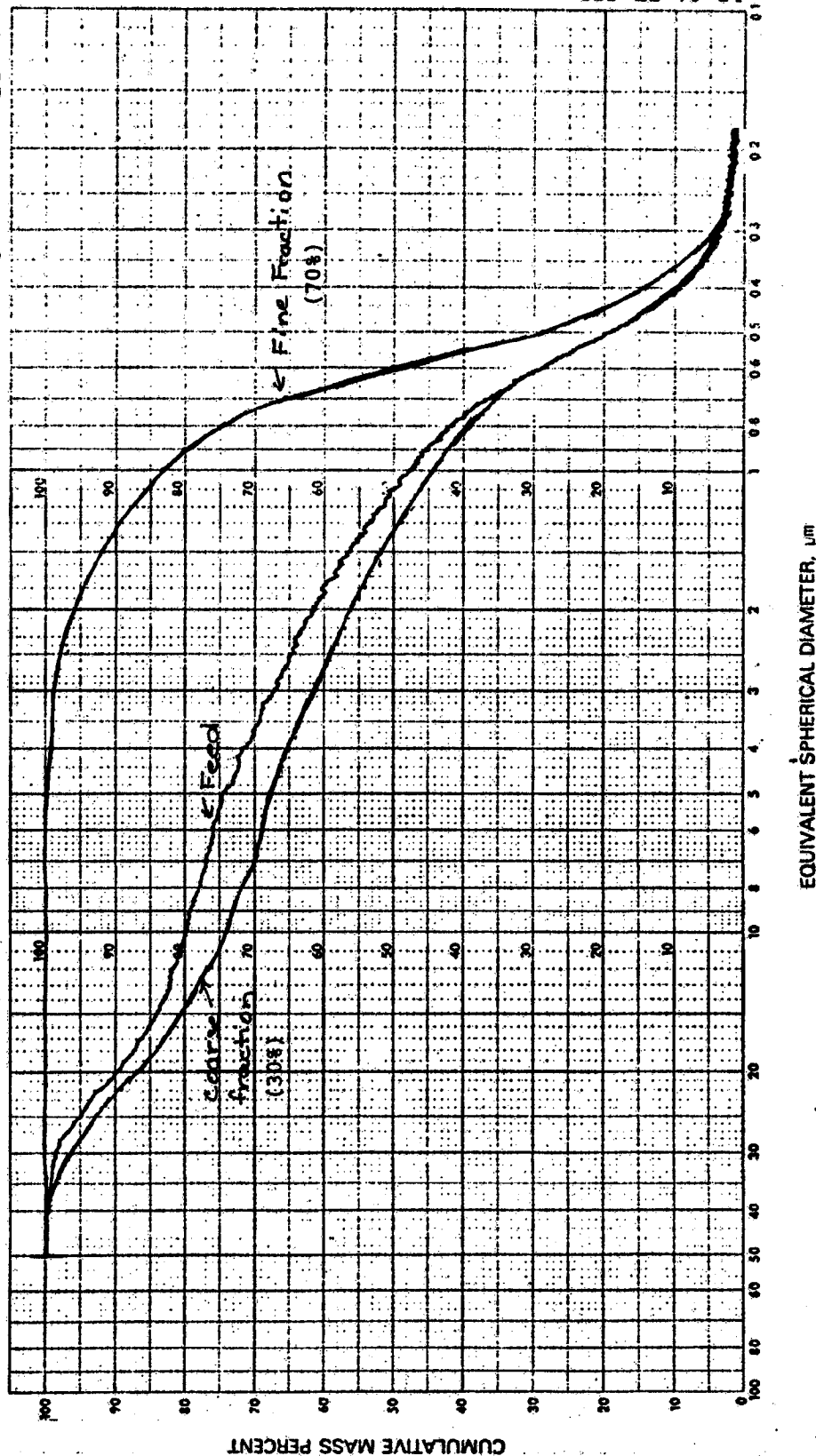


Figure 1341-11 PARTICLE SIZE DISTRIBUTION

SAMPLE IDENTIFICATION Uternal Jet Classification of R900 **LSW** DATE **11-29-78** **3**
 Density **4.11** g/cc LIQUID **H₂O-TMPP** Density **0.9954** g/cc Viscosity **0.0840** cp BY **CLS** TS
 Preparation **Std.** Classified at **200 kg/hr.** TEMPERATURE **31** °C RATE **215** START DIA **50**



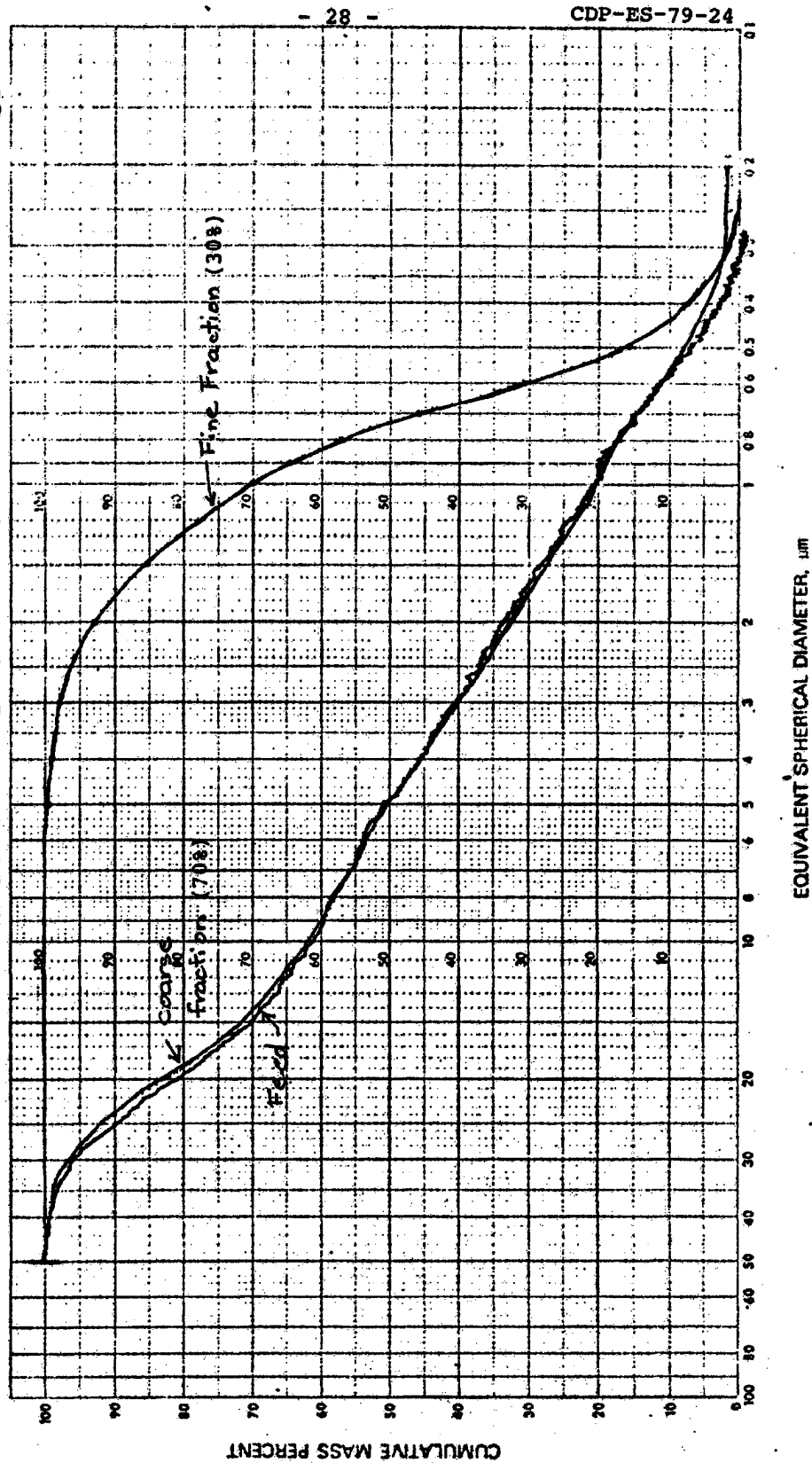
micromeritics
 instrument corporation
 5090 graham square north charleston, georgia 29405

Form 503/4770

Figure LSW-12

PARTICLE SIZE DISTRIBUTION

SAMPLE IDENTIFICATION **GC-4** Urtural Jet Classification of R931 **LSW** DATE **12-1-78** ②
 Density **3.86** g/cc LIQUID **H₂O-THPP-P** Density **0.9954** g/cc Viscosity **0.7840** cp BY **CRB** TS
 Preparation **8+d**, Classified at **360 kg/hr.** TEMPERATURE **31** °C RATE **198** START DIA **50**



m micromeritics
 INSTRUMENT CORPORATION
 4400 W. 10th Street, Lincoln, Nebraska 68502

Figure LSW-13

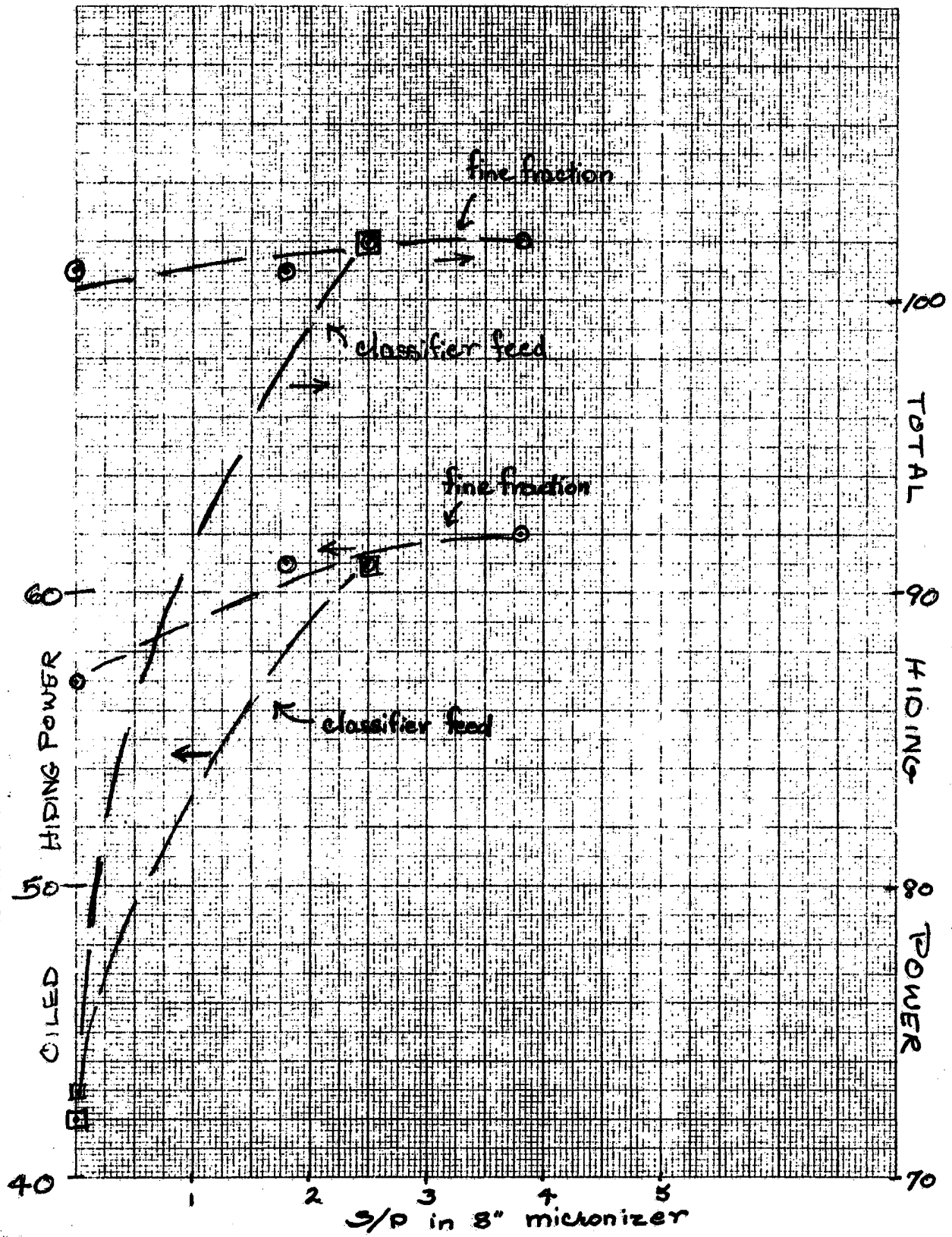


FIGURE LSW-14

B. G. NEWMAN'S COANDA-FLOW CONFIGURATION

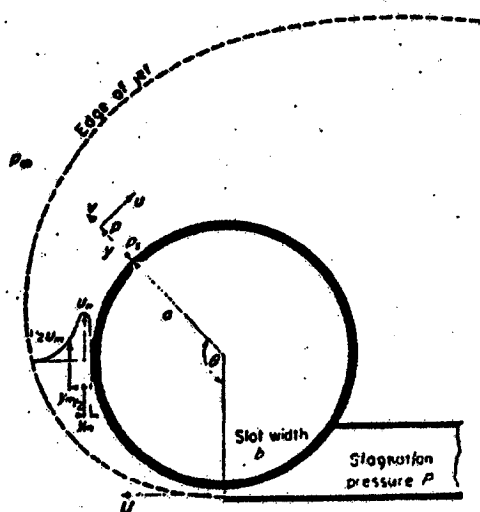


Figure LSW-15
 PARTICLE TRAJECTORIES
 6" Radius of Curvature
 2" Slot Height

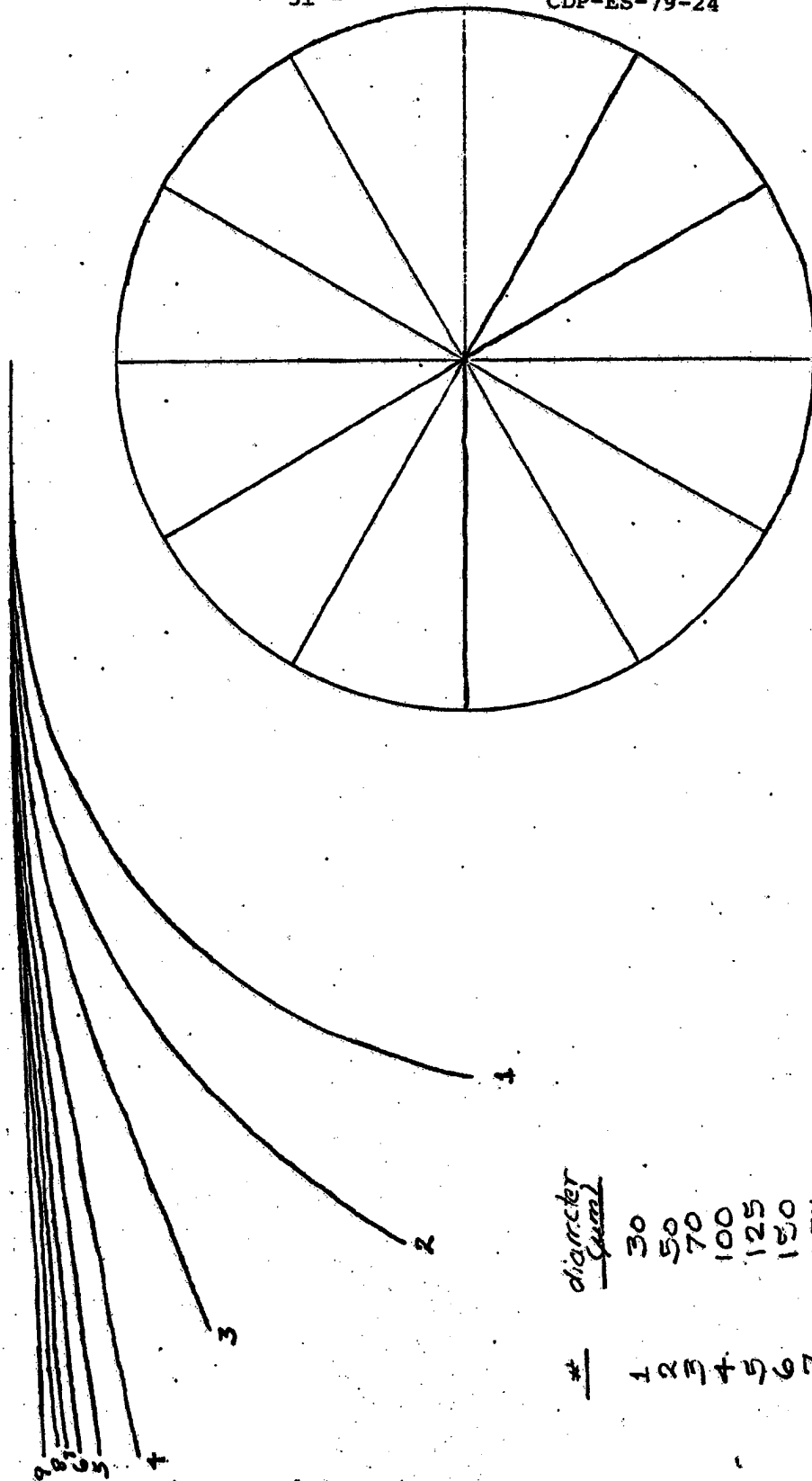
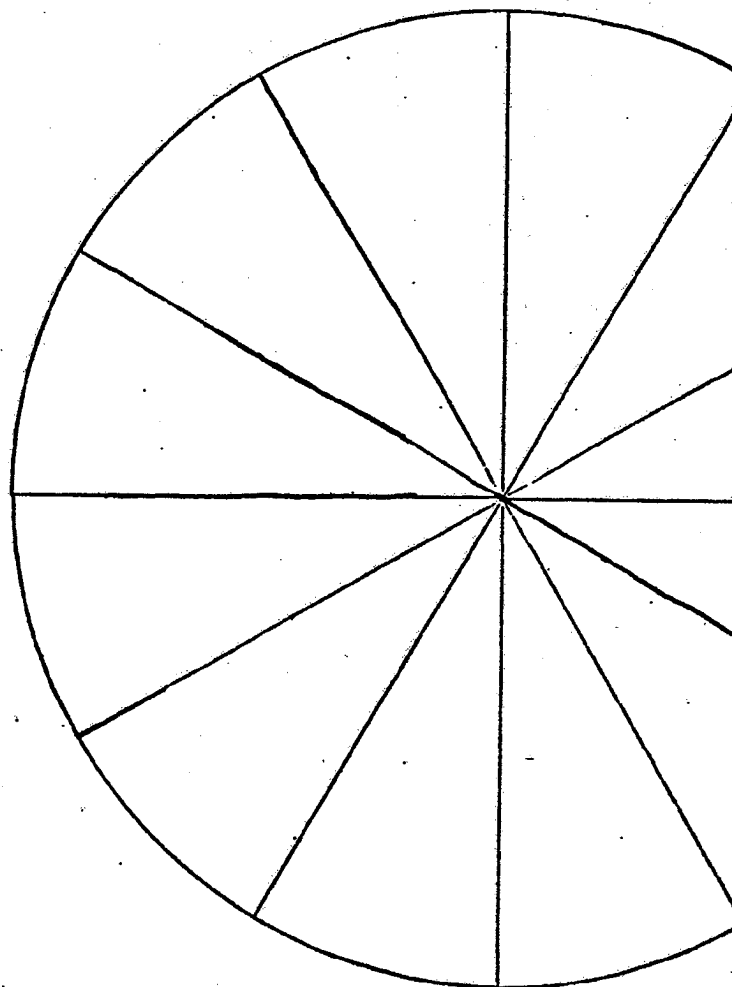
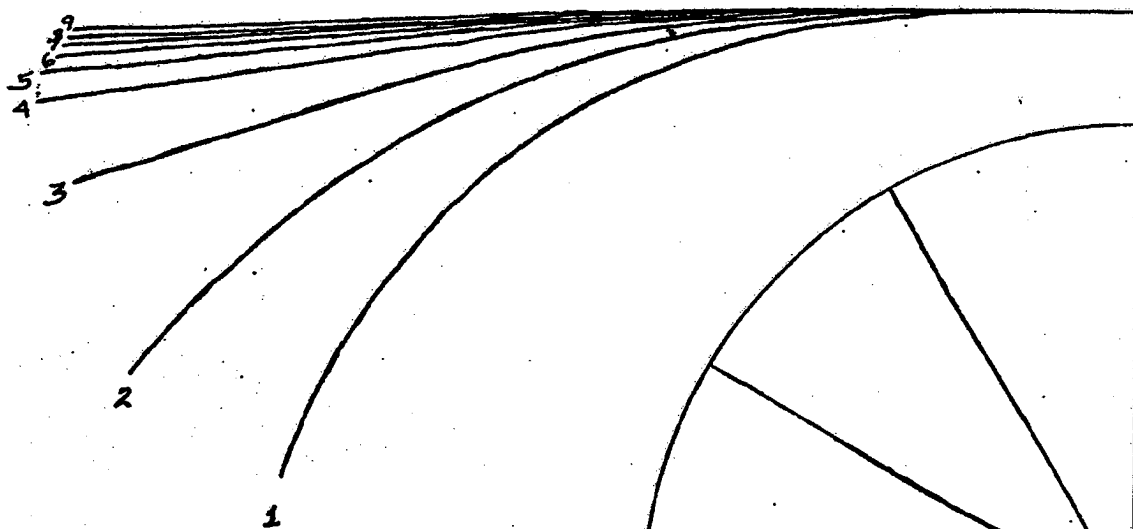


Figure LSW-16
PARTICLE TRAJECTORIES

8" Radius of Curvature, 2" Slot Height



#	diameter (μm)
1	30
2	50
3	70
4	100
5	125
6	150
7	175
8	200
9	250

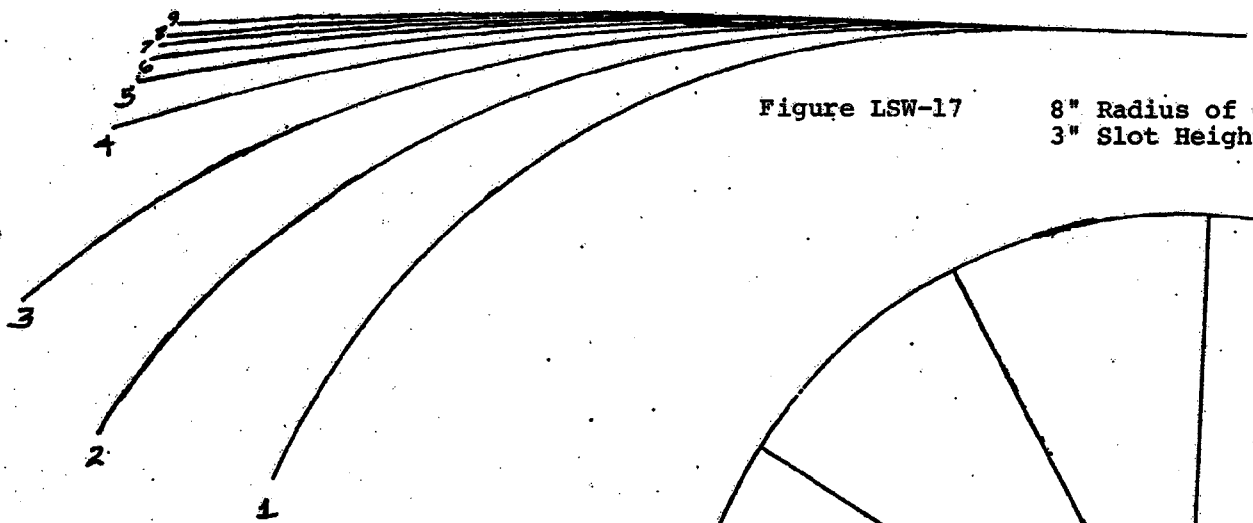
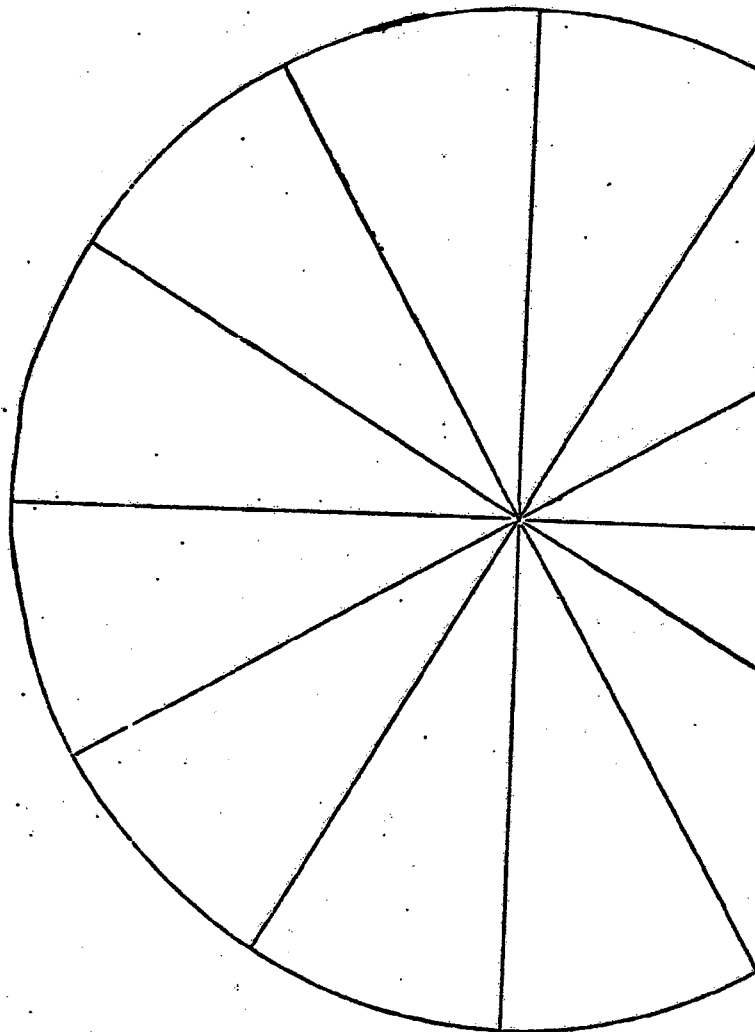


Figure LSW-17

8" Radius of Curvature
3" Slot Height



#	diameter (μm)
1	30
2	50
3	70
4	100
5	125
6	150
7	175
8	200
9	250

Figure LSW-18
 6" Radius of Curvature
 2" Slot Height

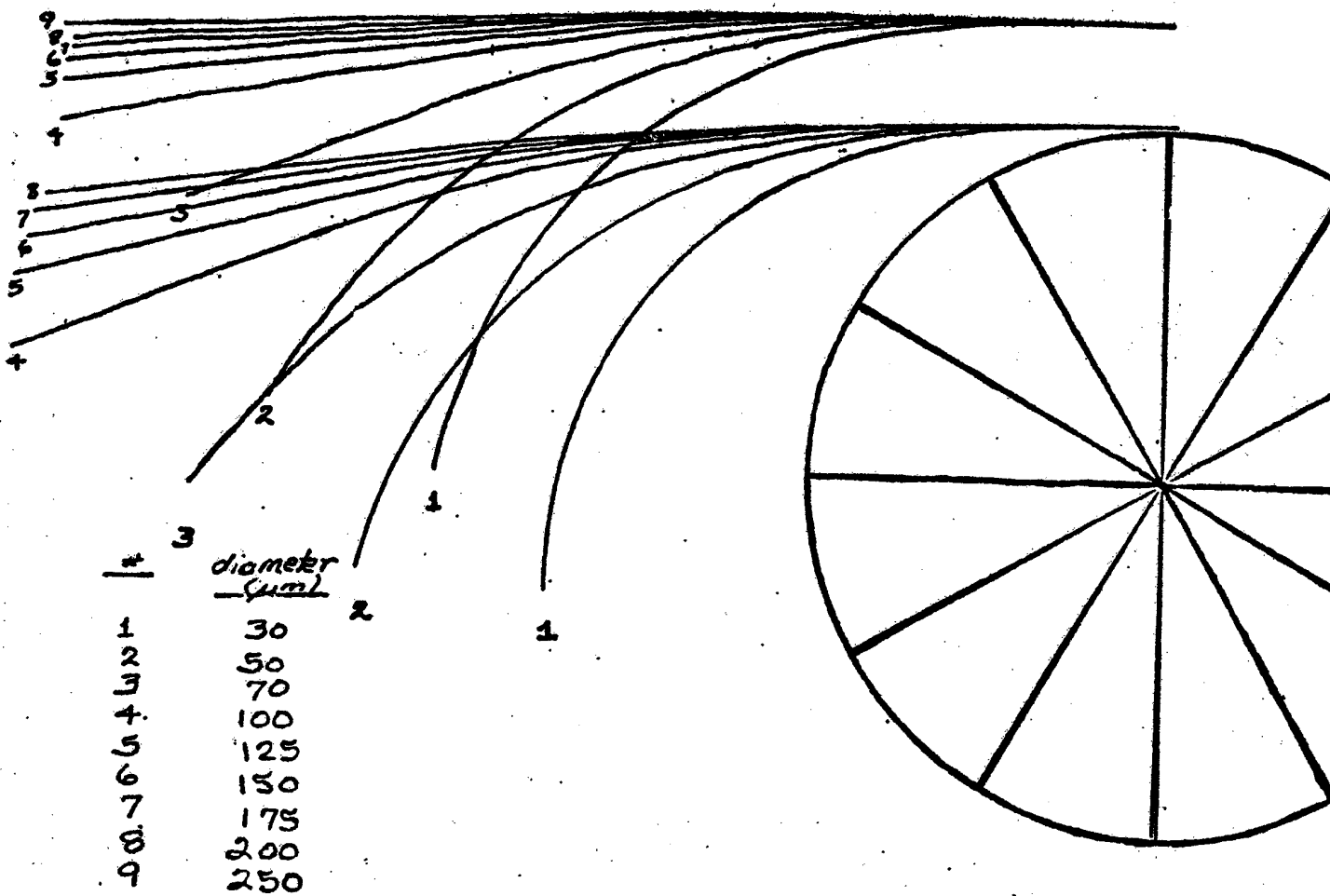
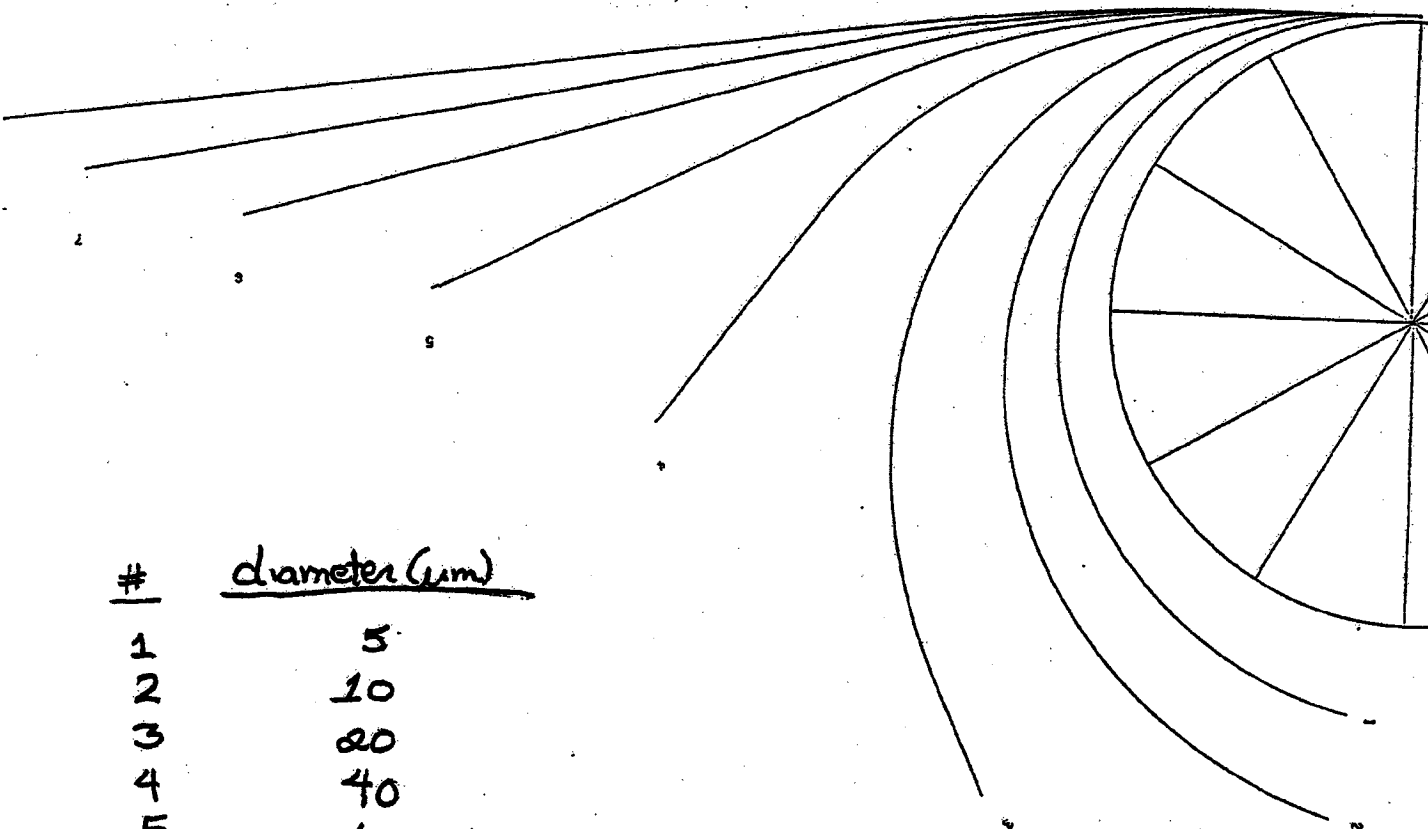


Figure LSW-19

UTERNAL JET DESIGN
4" Radius of Curvature
2" Feed Slot

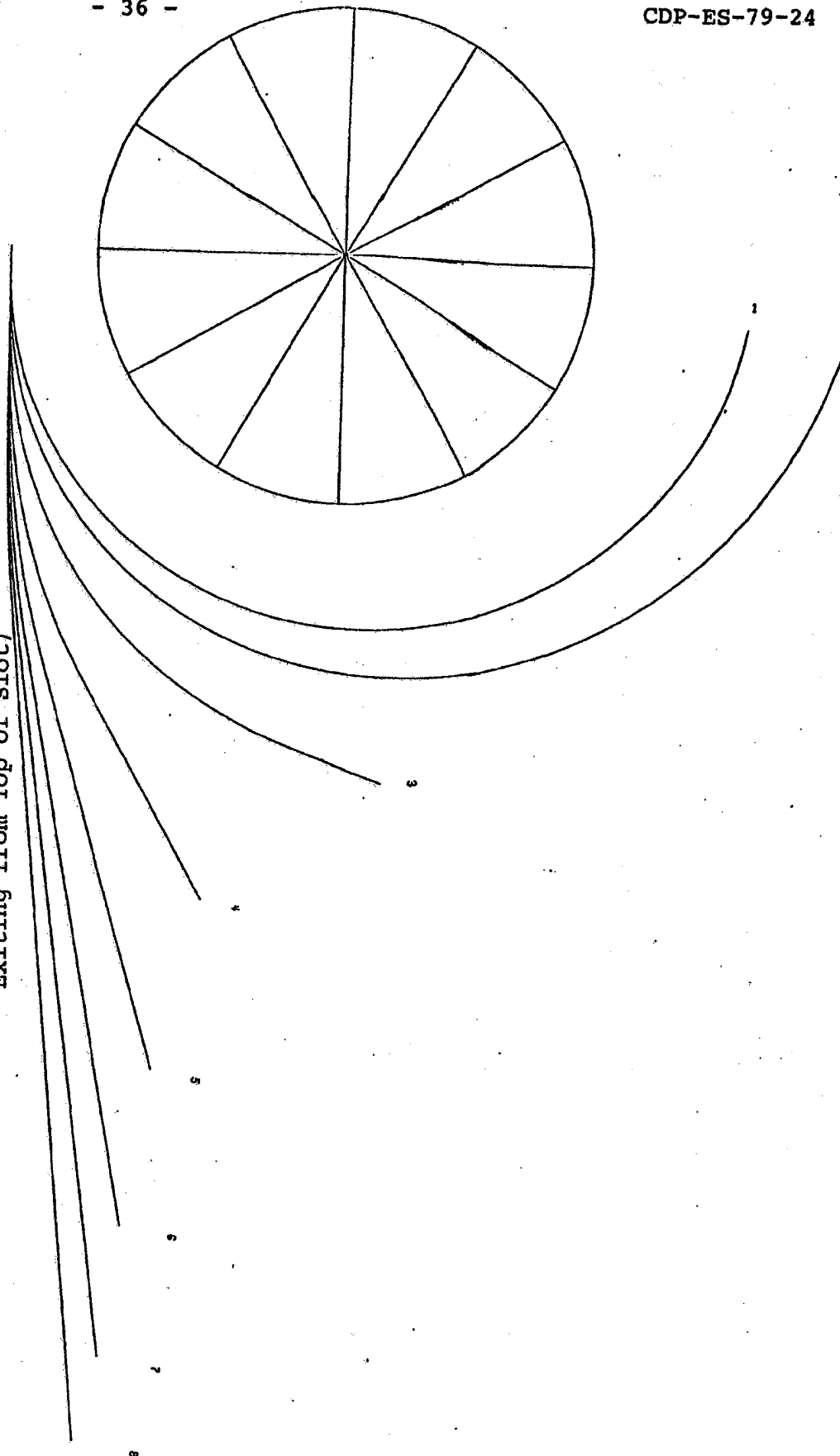


#	diameter (um)
1	5
2	10
3	20
4	40
5	60
6	80
7	100
8	125

Figure LSW-20

UTERNAL JET

(Same as Figure LSW-19 Except
Exiting from Top of Slot)



APPENDIX: COMPUTER PROGRAM

```

00 R 001677 VNER      0000 R 001671 VNET      0000 R 001702 VNU      0000 R 001700
00 R 001637 VRET      0000 R 001653 XB       0000 R 001663 XC       0000 R 001646
00 R 001703 XXX       0000 R 000000 Y        0000 R 001720 YY      0000 R 001704

```

```

1*      COMMON INT,AT,BT,CT,DT,KAY1,KAY2,KAY3,KAY4
2*      DIMENSION Y(3),RR(300),THETA(300),V(300),ITR(9)
3*      REAL KAY1,KAY2,KAY3,KAY4
4*      DATA ITR/'1','2','3','4','5','6','7','8','9'/
5*      C      VIN      = INITIAL PARTICLE VELOCITY (CM/SEC)
6*      C      DM       = PARTICLE DIAMETER (MICRONS)
7*      C      TM       = GAS TEMPERATURE (C)
8*      C      VISC     = GAS VISCOSITY (POISE)
9*      C      RHOP     = DENSITY OF PARTICLE (GM/CM3)
10*     C      RHOG     = DENSITY OF GAS (GM/CM3)
11*     C      RIN      = RADIUS OF CURVATURE OF COANDA SURFACE (CM)
12*     C      VRET     = TANGENTIAL VELOCITY OF PARTICLE (CM/SEC)
13*     C      SLOT     = PIGMENT FEED SLOT HEIGHT (CM)
14*     C      TDEL     = TIME STEP FOR CALCULATIONS (SEC)
15*     C      PST      = STARTING LOCATION OF PARTICLE IN SLOT (0.0 TO 1.0,
16*     C                  0.0 SETS PARTICLE AT SURFACE, 1.0 SETS PARTICLE AT
17*     C                  TOP OF SLOT)
18*
19*     C      NUM = 0
20*     C      DRAW COANDA SURFACE
21*     C      CALL PLOTS(0,0,0)
22*     C      CALL PLOT(2.0,2.0,3)
23*     C      CALL ORIGIN (8.0,8.0,-1)
24*     C      CALL SCALF (0.394,0.394,1)
25*     C      ADD SPOKES TO INDICATE ANGLES
26*     C      READ (5,100) SLOT,VIN,VISC,TM,RHOG,RIN,TDEL,PST
27*     C      CALL POL(0.,0.,PIN,12,1,0)
28*     C      100 FORMAT (8F10.0)
29*     C      102 READ(5,100) DM,RHOP
30*     C      IF (DM) 999,999,150
31*     C      150 WRITE (6,104) SLOT,VIN,DM,VISC,TM
32*     C      104 FORMAT (1H1///10X,'SLOT =',F8.2,5X,'VIN =',F8.2,5X,'DM =',
33*     C      1 F6.2,5X,'VISC =',F7.4,5X,'TM =',F5.0)
34*     C      WRITE (6,105) RHOP,RHOG,RIN,TDEL
35*     C      105 FORMAT (9X,'RHOP =',F5.1,5X,'RHOG =',F6.3,5X,'RIN =',F6.2,5X,
36*     C      1 'TDEL =',F8.5)
37*     C      SET INITIAL POSITION OF PARTICLE
38*     C      RR(1) = RIN + PST*SLOT
39*     C      VGAS = VIN
40*     C      TT = 0.0
41*     C      Y(1) = 0.0
42*     C      Y(2) = PR(1)
43*     C      Y(3) = 0.
44*     C      V(1) = Y(1)
45*     C      THETA(1) = Y(3)
46*     C      RAD = DM/2.
47*     C      VREP = 0.
48*     C      VPFT = VIN
49*     C      T1 = 0.375*PHOG
50*     C      T2 = RAD*PHOP*1.E-4
51*     C      RER = RHOG*DM*1.E-4/VISC
52*     C      J = 1

```

```

52*      INT = 1
53*      C      DETERMINE GAS VELOCITY AT PRESENT PARTICLE POSITION
54*      200  CALL AGAST (RR(J),THETA(J),VIN,VGAS)
55*      IF (VGAS.LE.1.0) GO TO 500
56*      RE = REW*ABS(VRET - VGAS)
57*      J = J + 1
58*      VAN = SORT(VRET*VRET + VRER*VRER)
59*      XV = VAN*TOEL
60*      TH = ATAN(VRER/VRET)
61*      RR(J) = SORT(XV*XV + RR(J-1)*RR(J-1) - 2.0*XV*RR(J-1)*COS(1.57+TH
62*      1 )
63*      THA = ASIN(XV*SIN(1.57+TH)/RR(J))
64*      THETA(J) = THA + THETA(J-1)
65*      C      CALCULATE DRAG COEFFICIENT
66*      201  IF (DM.LE.1.3.OR.RE.LE.0.1) CD=24./RER
67*      IF (DM.GT.1.3.AND.RE.GT.0.1) GO TO 204
68*      IF (DM.GT.1.3) GO TO 202
69*      CUNN = 1.0 + (.0002*TH/DM)*(2.79+0.894*EXP(-2.47E3*DM/TH))
70*      CD = CD/CUNN
71*      202  XB = T1*CD/T2
72*      IF (XB*TT.LT.50.0) GO TO 203
73*      IF (INT.EQ.2) GO TO 302
74*      GO TO 301
75*      203  BT = XB
76*      CT = VGAS
77*      AT = (VRET - CT)/EXP(-BT*TT)
78*      C      EQUATION FORM V=A*EXP(-B*T) + C
79*      GO TO 300
80*      204  IF (RE.GT.3.0) GO TO 206
81*      C1 = 0.0
82*      C2 = 24./RER
83*      C3 = 2.4
84*      GO TO 208
85*      206  IF (RE.GT.100.) GO TO 207
86*      C1 = -17.5/RER/RER
87*      C2 = 34.6/RER
88*      C3 = 0.815
89*      GO TO 208
90*      207  C1 = 0.0
91*      C2 = 75./RER
92*      C3 = 0.4
93*      208  TN1 = (T1*C1 - T1*C2*VGAS + T1*C3*VGAS*VGAS)/T2
94*      TN2 = (T1*C2 - 2.*T1*C3*VGAS)/T2
95*      TN3 = (T1*C3)/T2
96*      Q = TN2*TN2 - 4.*TN1*TN3
97*      C      EQUATION FORM V = A/(1. - B*EXP(-CT)) + D
98*      XC = SQRT(Q)
99*      IF (XC*TT.GE.50.0) GO TO 345
100*      DT = -(TN2 + SQRT(Q))/TN3/2.0
101*      AT = SQRT(Q)/TN3
102*      CT = XC
103*      BT = (1.0 - AT/(VRET - DT))/EXP(-CT*TT)
104*      IF (INT.EQ.2) GO TO 210
105*      ATA = AT
106*      BTH = BT
107*      CTC = CT
108*      DTD = DT
109*      341  TW = TT + TDEL

```

```

110*      VNET = ATA/(1.0 - BTB*EXP(-CTC*TW)) + DTD
111*      INT = 2
112*      GV = VGAS
113*      VGAS = 0.0
114*      VRET = VRER
115*      RE = RER*VRER
116*      GO TO 201
117*      345 IF (INT.EQ.2) GO TO 343
118*      GO TO 341
119*      210 ATT = AT
120*      BTT = BT
121*      CTT = CT
122*      DTT = DT
123*      343 TT = TW
124*      VNER = ATT/(1.0 - BTT*EXP(-CTT*TT)) + DTT
125*      INT = 1
126*      GO TO 350
127*      300 IF (INT.EQ.2) GO TO 340
128*      ATA = AT
129*      BTB = BT
130*      CTC = CT
131*      301 TW = TT + TDEL
132*      VNET = ATA*EXP(-BTB*TW) + CTC
133*      INT = 2
134*      GV = VGAS
135*      VRET = VRER
136*      VGAS = 0.0
137*      RE = RER*VRER
138*      GO TO 201
139*      340 ATT = AT
140*      BTT = BT
141*      CTT = CT
142*      302 TT = TW
143*      VNER = ATT*EXP(-BTT*TT) + CTT
144*      INT = 1
145*      350 VN1 = SORT(VNET*VNET + VNER*VNER)
146*      TH2 = ATAN(VNER/VNET)
147*      VRET = VN1*COS(TH2 + THA)
148*      VRER = VN1*SIN(TH2 + THA)
149*      V(J) = VN1
150*      IF (THETA(J).GE.3.0.DF.PR(J).GE.50.0) GO TO 400
151*      IF (J.EQ.300) GO TO 400
152*      IF (V(J).LE.10.0) GO TO 400
153*      GO TO 200
154*      C DETERMINE TRAJECTORIES FOR PARTICLES WHICH HAVE ESCAPED HIGH-
155*      C VELOCITY GAS STREAM
156*      500 VNU = SORT(VRET*VPET + VRER*VRER)
157*      XXX = PR(J)*SIN(THETA(J))
158*      YYY = PR(J)*COS(THETA(J))
159*      PHI = ATAN(VRER/VPET)
160*      PSI = THETA(J) - PHI
161*      501 RE = RER*VNU
162*      C CALCULATE DRAG COEFFICIENT
163*      IF (DM.LE.1.3.OR.PE.LE.0.1) CD = 24./REP
164*      IF (DM.GT.1.3.AND.RE.GT.0.1) GO TO 504
165*      IF (DM.GT.1.3) GO TO 502
166*      CUMN = 1.0 + (.0002*T*/DM)*(2.79+0.894*EXP(-2.47E3*DM/T*))
167*      CD = CD/CUMN

```

```

168*      502 XB = T1*CD/T2
169*      IF (XB*TT.GE.50.0) GO TO 550
170*      BT = XB
171*      CT = 0.0
172*      AT = (VNU - CT)/EXP(-BT*TT)
173*      550 T = TT
174*      TT = TT + TDEL
175*      VNU = AT*EXP(-BT*TT) + CT
176*      AA = -AT*COS(PSI)/BT
177*      BB = BT
178*      CC = CT*COS(PSI)
179*      DD = XXX-AA*EXP(-BB*T) - CC*T
180*      XXX = AA*EXP(-BB*TT) + CC*TT + DD
181*      AA = AT*SIN(PSI)/BT
182*      CC = -CT*SIN(PSI)
183*      DD = YYY - AA*EXP(-BB*T) - CC*T
184*      YYY = AA*EXP(-BB*TT) + CC*TT + DD
185*      J = J + 1
186*      RR(J) = SQRT(XXX*XXX + YYY*YYY)
187*      THETA(J) = ATAN(XXX/YYY)
188*      IF (THETA(J).LT.0.0) THETA(J) = THETA(J) + 3.14
189*      V(J) = VNU
190*      IF (THETA(J).GE.3.0.OR.RR(J).GE.50.0) GO TO 400
191*      IF (J.EQ.300) GO TO 400
192*      IF (V(J).LE.10.0) GO TO 400
193*      GO TO 501
194*      504 IF (RE.GT.3.0) GO TO 506
195*      C1 = 0.0
196*      C2 = 24.0/RER
197*      C3 = 2.4
198*      GO TO 508
199*      506 IF (RE.GT.100.) GO TO 507
200*      C1 = -17.5/RER/RER
201*      C2 = 34.6/RER
202*      C3 = 0.815
203*      GO TO 508
204*      507 C1 = 0.0
205*      C2 = 75.0/RER
206*      C3 = 0.4
207*      508 TN1 = T1*C1/T2
208*      TN2 = T1*C2/T2
209*      TN3 = (T1*C3)/T2
210*      Q = TN2*TN2 - 4.*TN1*TN3
211*      XC = SQRT(Q)
212*      IF (XC*TT.GE.50.0) GO TO 552
213*      DT = -(TN2 + SQRT(Q))/TN3/2.0
214*      AT = SQRT(Q)/TN3
215*      CT = XC
216*      BT = (1.0 - AT/(VNU - DT))/EXP(-CT*TT)
217*      552 T = TT
218*      TT = TT + TDEL
219*      VNU = AT/(1.0 - BT*EXP(-CT*TT)) + DT
220*      AA = AT*COS(PSI) + DT*COS(PSI)
221*      BB = AT*COS(PSI)/CT
222*      CC = XXX - AA*T - BB*ALOG(1.0 - BT*EXP(-CT*T))
223*      XXX = AA*TT + BB*ALOG(1.0 - BT*EXP(-CT*TT)) + CC
224*      AA = -AT*SIN(PSI) - DT*SIN(PSI)
225*      BB = -AT*SIN(PSI)/CT

```

```

226*      CC = YYY - AA*T - BB*ALOG(1.0 - BT*EXP(-CT*T))
227*      YYY = AA*TT + BB*ALOG(1.0 - BT*EXP(-CT*TT)) + CC
228*      J = J + 1
229*      RR(J) = SORT(XXX*XXX + YYY*YYY)
230*      THETA(J) = ATAN(XXX/YYY)
231*      IF (THETA(J).LT.0.0) THETA(J) = THETA(J) + 3.14
232*      V(J) = VNU
233*      IF (THETA(J).GE.3.0.OR.RR(J).GE.50.0) GO TO 400
234*      IF (J.EQ.300) GO TO 400
235*      IF (V(J).LE.10.0) GO TO 400
236*      GO TO 501
237*      400 NPT = J
238*      C PLOT TRAJECTORY
239*      CALL POLAR(RR,THETA,NPT,1,0,1H*,0.,0.394)
240*      NUM = NUM + 1
241*      LAB = ITR(NUM)
242*      TEND = THETA(NPT) + 0.05
243*      XX = RR(NPT)*COS(TEND)
244*      YY = RR(NPT)*SIN(TEND)
245*      CALL CHAR(XX,YY,TEND,0.125,LAB,1)
246*      WRITE (6,106) (V(I),RR(I),THETA(I),I=1,NPT)
247*      106 FORMAT(1H1,(10X,F8.2,5X,F8.2,5X,F8.2))
248*      GO TO 102
249*      999 CALL PLOT(0.0,0.0,999)
250*      STOP
251*      END

```

END OF COMPILATION: NO DIAGNOSTICS.

A.
27R3A E35 SL73R1 11/27/79 13:48:52

S*COANDA(1) ELEMENT TABLE

E	VERSION	TYPE	DATE	TIME	SEQ #	SIZE-PRE,TEXT
B		FOR SYMB	30 DEC 77	11:11:30	1	19
S		FOR SYMB	05 JAN 78	09:07:10	2	7
S		FOR SYMB	10 JAN 78	11:00:57	3	4
		FOR SYMB	10 JAN 78	16:03:42	4	3
		FOR SYMB	10 JAN 78	16:03:49	5	3
		RELOCATABLE	11 JAN 78	09:49:51	6	1 3
		RELOCATABLE	11 JAN 78	09:49:54	7	1 3
B		RELOCATABLE	11 JAN 78	09:49:59	8	1 23
S		RELOCATABLE	11 JAN 78	09:50:02	9	1 4
S		RELOCATABLE	11 JAN 78	09:50:05	10	1 10
ST		FOR SYMB	21 NOV 79	11:21:01	11	2
ST		RELOCATABLE	21 NOV 79	11:21:06	12	1 2
NDA		FOR SYMB	26 NOV 79	13:03:44	13	61
NDA		RELOCATABLE	26 NOV 79	13:03:50	14	3 79
NDA		FOR SYMB	27 NOV 79	13:48:50	15	63
NDA		RELOCATABLE	27 NOV 79	13:48:52	16	3 76

AVAILABLE LOCATION-

LER PROCEDURE TABLE EMPTY

PROCEDURE TABLE EMPTY

COPE*GRAPH.POL,TPFS.POL
4R1 T -08/23/79-14:24:19 (1,)

ROUTINE POL ENTRY POINT 000253

RAGE USED: CODE(1) 000303; DATA(0) 000065; BLANK COMMON(2) 000000

TERNAL REFERENCES (BLOCK, NAME)

003 PLOT
004 PLTLN
005 NUMPLT
006 ELIPS
007 RMATHS
010 COSS
011 SINS

RAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

001	000073	123G	0001	000213	147G	0001	000133	2L	0001	00017
000 R	000012	BS	0000 R	000011	BY	0000 R	000002	C	0000 R	00001
000 R	000017	D	0000 R	000013	OS	0000	000023	DYNS	0000 I	00001
000 R	000006	RX	0000 R	000007	RY	0000 R	000003	S	0000 R	00001
000 R	000004	XS	0000 R	000020	XX	0000 R	000005	YS	0000 R	00002

```

1* SUBROUTINE POL(X,Y,R,NR,NC,IOP)
2* T = 360.0/NR
3* RA = .0174533
4* C = COS(RA*T)
5* S = SIN(RA*T)
6* CALL PLOT (XS,YS,4)
7* XS = 1.0
8* YS = 1.0
9* RX = R*XS
10* RY = R*YS
11* AX = RX/NC
12* BY = RY/NC
13* BS = .12
14* OS = R + .05
15* CC = C
16* SS = S
17* DO 4 I = 1,NR
18* CALL PLILN(X,Y,X+RX*CC,Y+RY*SS)
19* IF(IOP.EQ. 0) GO TO 3
20* D = T-I-90
21* IF(D-90.0) 2,2,1
22* 1 OS = R + .13
23* D = D + 180
24* BS = -.12
25* 2 XX = X + (OS*CC+OS*SS)*XS
26* YY = Y + (OS*SS-BS*CC)*YS

```

```
27*      CALL NUMPLT(XX,YY,RA*D,-.08,T*I,-1)
28*      3 CT = C*CC - S*SS
29*      SS = S*CC + C*SS
30*      4 CC = CT
31*      DO 5 I = 1,NC
32*      5 CALL ELIPS (X+AX*I,Y,AX*I,BY*I,0.,0.,0.,3)
33*      RETURN
34*      END
```

END OF COMPILATION: NO DIAGNOSTICS.

S A.AGAS,A.AGAS
0T3-01/11/78-09:49:59 (2,)

ROUTINE AGAS ENTRY POINT 000050

ORAGE USED: CODE(1) 000062; DATA(0) 000010; BLANK COMMON(2) 000000

ORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

001 000037 150L 0001 000044 152L 0001 000045 999L 0000 R 00000
000 R 000001 VH

```
1*      SUBROUTINE AGAS(R,TH,SLW,RAD,VI,VG)
2*      IF (TH.EQ.0.0) GO TO 999
3*      ALEN = 2.0*SLW*TH + SLW
4*      IF (R-RAD.LE.ALEN) GO TO 150
5*      IF (R-RAD.GE.1.25*ALEN) GO TO 152
6*      VH = VI*SLW/ALEN
7*      VG = -4.0*VH*(R-RAD-ALEN)/ALEN + VH
8*      GO TO 999
9*      150 VG = VI*SLW/ALEN
10*     GO TO 999
11*     152 VG = 0.0
12*     999 RETURN
13*     END
```

END OF COMPILATION: NO DIAGNOSTICS.

IS A.AGAST, AGAST
073-03/20/79-14:11:49 (.0)

BRROUTINE AGAST ENTRY POINT 000015

ORAGE USED: CODE(1) 000024; DATA(0) 000003; BLANK COMMON(2) 000000

ORAGE ASSIGNMENT (BLOCK, TYPE, RELATIVE LOCATION, NAME)

001 000010 150L 0001 000012 999L 0000 000000 DYN5

```

1*      SUBROUTINE AGAST(R,TH,VI,VG)
2*      IF (TH.EQ.0.0) GO TO 999
3*      IF (R.LE.5.00) GO TO 150
4*      VG = 0.0
5*      GO TO 999
6*      150 VG = VI
7*      999 RETURN
8*      END
    
```

END OF COMPILATION: NO DIAGNOSTICS.

F A.
2 27R3-1 E35 SL73R1 03/20/79 14:11:52

VS*COANDA(1) ELEMENT TABLE

4E	VERSION	TYPE	DATE	TIME	SEQ #	SIZE-PRE,TEXT
1B		FOR SYMB	30 DEC 77	11:11:30	1	19
1S		FOR SYMB	05 JAN 78	09:07:10	2	7
1S		FOR SYMB	10 JAN 78	11:00:57	3	4
		FOR SYMB	10 JAN 78	16:03:42	4	3
		FOR SYMB	10 JAN 78	16:03:49	5	3
		RELOCATABLE	11 JAN 78	09:49:51	6	1 3
		RELOCATABLE	11 JAN 78	09:49:54	7	1 3
1B		RELOCATABLE	11 JAN 78	09:49:59	8	1 23
1S		RELOCATABLE	11 JAN 78	09:50:02	9	1 4
1S		RELOCATABLE	11 JAN 78	09:50:05	10	1 10
1NDA		FOR SYMB	28 JUN 78	14:17:36	11	55
1NDA		RELOCATABLE	28 JUN 78	14:17:54	12	3 76
1NDA		FOR SYMB	20 MAR 79	14:11:47	13	56
1NDA		RELOCATABLE	20 MAR 79	14:11:49	14	3 76
1ST		FOR SYMB	20 MAR 79	14:11:50	15	2
1ST		RELOCATABLE	20 MAR 79	14:11:51	16	1 2

AVAILABLE LOCATION

3LER PROCEDURE TABLE EMPTY

PROCEDURE TABLE EMPTY

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