

where

$h_c$  = pressure loss due to sudden contraction, feet of fluid flowing.

$v'_2$  = the velocity at the vena contracta, feet per second.

$A'_2$  = the area of the vena contracta, square feet.

Introduction of the contraction coefficient  $\alpha = \frac{A'_2}{A_1}$  and the loss coefficient

$C = \left(\frac{1}{\alpha} - 1\right)^2$  in Equation 8 gives (with  $A'_2 \times v'_2 = A_1 \times v_1$ ):

$$h_c = C \frac{v_1^2}{2g} \quad (9)$$

or for standard air:

$$H_c = C \left(\frac{V_1}{4005}\right)^2 \quad (10)$$

where

$H_c$  = pressure loss due to sudden contraction, inches of water.

$V_1$  = velocity of standard air in the inlet duct, in feet per minute.

Values of  $\alpha$  and  $C$  for sharp corners for increasing ratios of  $A_2/A_1$  are given in the following table:

| $A_2/A_1$ | 0.01 | 0.1  | 0.2  | 0.4  | 0.6  | 0.8  | 1.00 |
|-----------|------|------|------|------|------|------|------|
| $\alpha$  | 0.6  | 0.61 | 0.62 | 0.65 | 0.7  | 0.77 | 1.00 |
| $C$       | 0.44 | 0.41 | 0.37 | 0.29 | 0.19 | 0.09 | 0.00 |

For discharge to atmosphere from a pipe,  $C = 1.0$  in Equation 10.

For a gradual enlargement, Equation 7 changes to

$$H_{e.c.} = C_1 \left(\frac{V_1 - V_2}{4005}\right)^2 \quad (11)$$

where

$H_{e.c.}$  = pressure loss due to gradual enlargement, based on standard air, inches of water.

$C_1$  = coefficient of loss, dependent upon the total angle included between the sides of the duct.

Values for  $C_1$  are given in the following table:

| TOTAL INCLUDED ANGLE, DEGREES | 5    | 7    | 10   | 20   | 30   | 40   | 50   | 60  |
|-------------------------------|------|------|------|------|------|------|------|-----|
| $C_1$                         | 0.20 | 0.15 | 0.16 | 0.35 | 0.65 | 0.80 | 0.92 | 1.0 |

Pressure losses for various duct transitions and area changes have been determined experimentally, although the available information is generally restricted to symmetrical area changes.<sup>6, 7, 14, 15, 16, 17</sup>

### PRESSURE CHANGES

The fundamental energy equation for standard air flow in a horizontal duct can be written<sup>18</sup>

$$H_1 + \left(\frac{V_1}{4005}\right)^2 = H_2 + \left(\frac{V_2}{4005}\right)^2 + \text{Loss of pressure (head), inches of water} \quad (12)$$

where

$H_1$  and  $H_2$  = the static pressure (head) at two given points (1) and (2), inches of water.

$\left(\frac{V_1}{4005}\right)^2$  and  $\left(\frac{V_2}{4005}\right)^2$  = the velocity pressure (head) at the same points, inches of water.

Equation 12 states that the mechanical energy at a given point (1) must be equal to the mechanical energy at another point (2), plus any dissipation of mechanical energy to internal energy (loss of pressure). Equation 12 is valid only if no work is done by or upon the air between the sections (1) and (2), and if there is no heat transfer to or from the air.

In Equation 12,  $H$  is a measure of the potential energy and  $\left(\frac{V}{4005}\right)^2$  a measure of the kinetic energy or energy of motion. The sum of static pressure and velocity pressure is called total pressure, and is a measure of the total energy.

Static pressure and velocity pressure are mutually convertible, that is to say, static pressure may be converted into velocity pressure, and vice versa. Every change in the cross-sectional area of a duct results in such a conversion of energy and is always accompanied by some loss in efficiency, or loss in total pressure.

In the final analysis of pressure losses in ducts, dynamic losses are due to accelerations and decelerations of the air stream as a whole. In a converging duct, the air velocity will be accelerated; some pressure head will be converted into velocity pressure. This conversion is generally a stable and efficient process, the energy losses are small, and there is no eddy formation.

In an expanding duct section, on the other hand, the air will be decelerated and an opposing pressure gradient be required to reduce the velocity. If the angle of divergence is appreciable, the flow becomes unstable, there is danger of separation of the flow from the duct wall, and large energy losses and eddy formation are possible.<sup>19</sup>

In order to keep losses in an expanding duct section to a minimum and to convert the velocity pressure efficiently into static pressure, the angle of divergence should be kept small.<sup>20</sup> Theoretically, it might seem possible to increase the duct area so gradually that the reduction in velocity and accompanying loss of velocity pressure would occur reversibly, and thus permit 100 percent conversion to static pressure. Such an ideal application of the principle of static regain in duct design is, of course, impossible for various reasons<sup>21</sup> such as: the necessity of using sections of uniform diameter because of cost, the need for using ducts of dimensions varying in full inches, the changing of duct sizes mainly at branch connections, and