

Tables 3 and 4 show properties of water for temperatures above 212 F. These tables were abstracted from the steam tables of Keenan and Keyes.⁴

DEGREE OF SATURATION AND ITS USE IN CALCULATIONS

At given values of temperature and pressure, the humidity ratio W of moist air may have any value between zero (dry air) and W_s (moist air at saturation). For convenience, a parameter μ called degree of saturation is introduced through the use of Equation 1.

$$W = \mu W_s \quad (1)$$

To a degree of approximation within the estimated uncertainty of data in Table 1, at temperatures below about 150 F, the volume v of moist air per pound of dry air may be computed by Equation 2.

$$v = v_a + \mu v_{ws} \quad (2)$$

To obtain comparable accuracy at temperatures above about 150 F, it is necessary to add a correction term δ as follows:

$$v = \frac{\mu(1 - \mu)A}{1 + 1.6078 \mu W_s} \quad (3)$$

At temperatures below 150 F, the enthalpy h of moist air per pound of dry air may be computed by Equation 4.

$$h = h_a + \mu h_{ws} \quad (4)$$

To obtain comparable accuracy at temperatures above about 150 F, it is necessary to add a correction term δ as follows:

$$h = \frac{\mu(1 - \mu)B}{1 + 1.6078 \mu W_s} \quad (5)$$

Unfortunately, values of entropy s of moist air per pound of dry air computed by the relation

$$s = s_a + \mu s_{ws} \quad (6)$$

do not approximate the true values as closely as might be desired except at temperatures considerably below 150 F. Only a small portion of the error is compensated for by the correction term

$$\delta = \frac{\mu(1 - \mu)C}{1 + 1.6078 \mu W_s} \quad (7)$$

The larger portion of the deviation arises from the mixing entropy. It can be expressed as an additional correction term as follows:

$$\delta = 0.1579 [(1 + 1.6078 \mu W_s) \log_{10} (1 + 1.6078 \mu W_s - 1.6078 \mu W_s \log_{10} \mu) - \mu(1 + 1.6078 W_s) \log_{10} (1 + 1.6078 W_s)] \quad (8)$$

Table 5 shows values of the coefficients A , B , and C in Equations 3, 5, and 7 respectively and maximum values of the correction terms δ , δ , and δ .

THERMODYNAMIC WET-BULB TEMPERATURE

For any state of moist air, there exists a temperature t^* at which liquid (or solid) water may be evaporated into the air to bring it to saturation at exactly this same temperature. Fig. 8 may be used as a schematic representation of the adiabatic saturation process where the leaving air is saturated and is at a temperature equal to that of the injected water. In the process, the humidity ratio is increased from a given initial value W to the value W_s corresponding to satu-

ration at the temperature t^* ; the enthalpy is increased from a given initial value h to the value h_s corresponding to saturation at the temperature t^* ; the weight of water added per pound of dry air is $(W_s - W)$ which adds energy to the moist air of amount $(W_s - W)h_s$, where h_s denotes the specific enthalpy of the water added at the temperature t^* . Therefore, if the process is strictly adiabatic, conservation of energy requires that:

$$h + (W_s - W)h_s = h_s \quad (9)$$

The properties W_s , h_s , and h_s are functions only of the temperature t^* for a fixed value of pressure. The value of t^* which satisfies Equation 9 for given values of h and W is called thermodynamic wet-bulb temperature.

The psychrometer is a device consisting of two thermometers, one of which has its bulb covered with a suitable wick that has been thoroughly wetted with water. When the wet bulb is placed in an air stream, water may evaporate from the wick. The equilibrium temperature eventually reached by the water is called the wet-bulb temperature. This process is not the same as one of adiabatic saturation which defines the thermodynamic wet-bulb temperature, but rather is one of simultaneous heat and mass transfer from the wet-bulb. The fundamental mechanism of this process is described in Chapter 5, Mass Transfer. Fortunately, and indeed fortuitously, the corrections to be applied to readings of a wet-bulb thermometer to obtain the thermodynamic wet-bulb temperature are usually quite small. Arnold⁵ has presented a procedure which allows calculation of these corrections:

Example 1: Find the degree of saturation, humidity ratio, enthalpy, and volume of moist air at 90 F dry-bulb temperature, 63 F thermodynamic wet-bulb temperature, and 29.921 in. Hg pressure.

Solution: From Equations 1, 4, and 9.

$$(h_a + \mu h_{ws}) + (W_s - \mu W_s)h_s = h_s$$

Inserting numerical data from Table 1 gives:
(21.625 + 34.31 μ) + (0.01235 - 0.03118 μ)(31.12) = 28.57
and

$$\mu = 0.1967$$

From Equation 1

$$W = (0.1967)(0.03118) = 0.006133 \text{ lb. water/lb. dry air}$$

From Equation 4

$$h = 21.625 + (0.1967)(34.31) = 28.37 \text{ Btu/lb. dry air}$$

From Equation 2

$$v = 13.853 + (0.1967)(0.692) = 13.989 \text{ cu ft/lb. dry air}$$

PERFECT GAS RELATIONS

Tables 1 and 5, with Equations 1 to 9, allow accurate calculations of moist air properties where sea-level pressure may be assumed. The equations of Goff and Gratch may be used to calculate tables similar to Table 1 for any pressure, but, as yet such tables are not available. Fortunately, only slight errors occur when Dalton's Rule and perfect-gas relations are applied where normal barometric pressures exist.

According to Dalton's Rule, if dry air and water vapor are mixed, each occupies the whole volume of the container at the temperature of the mixture, and the pressure of the mixture is the sum of the individual pressures. Assuming that both dry air and water vapor behave like perfect gases, the volume v occupied by n_a mols of dry air at temperature T and pressure p_a is:

$$v = \frac{n_a RT}{p_a} \quad (10)$$

Table 1. Thermodynamic Properties of MOIST AIR* (Standard Atmospheric Pressure, 29.921 in. Hg)

Fahr. Temp. (°F)	Humidity Ratio $W_s \times 10^3$	Volume cu ft/lb dry air			Enthalpy Btu/lb dry air			Entropy Btu per (°F) lb dry air			Condensed Water			Fahr. Temp. (°F)
		v_a	v_{ws}	v_s	h_a	h_{ws}	h_s	s_a	s_{ws}	s_s	Enthalpy Btu/lb h_{ws}	Entropy Btu per (°F) lb s_{ws}	Vap. Press. in. Hg $p_s \times 10^3$	
-160	0.000110	7.530	0.000	7.530	-18.504	0.000	-18.504	-0.10300	0.00000	-0.10300	-222.00	-0.4807	0.0001009	-160
-155	0.000109	7.647	0.000	7.647	-17.796	0.000	-17.796	-0.09901	0.00000	-0.09901	-220.40	-0.4853	0.0001042	-155
-150	0.000108	7.715	0.000	7.715	-16.688	0.000	-16.688	-0.06628	0.00000	-0.06628	-218.77	-0.4920	0.0001083	-150
-145	0.000110	7.902	0.000	7.902	-14.811	0.000	-14.811	-0.05131	0.00000	-0.05131	-217.12	-0.4977	0.0001130	-145
-140	0.000109	8.079	0.000	8.079	-13.674	0.000	-13.674	-0.03740	0.00000	-0.03740	-215.44	-0.4995	0.0001180	-140
-135	0.000108	8.156	0.000	8.156	-12.456	0.000	-12.456	-0.02365	0.00000	-0.02365	-213.76	-0.4949	0.0001230	-135
-130	0.000106	8.233	0.000	8.233	-11.283	0.000	-11.283	-0.01000	0.00000	-0.01000	-212.03	-0.4890	0.0001280	-130
-125	0.000105	8.411	0.000	8.411	-10.057	0.000	-10.057	0.00364	0.00000	0.00364	-210.28	-0.4820	0.0001330	-125
-120	0.000104	8.587	0.000	8.587	-8.823	0.000	-8.823	0.01737	0.00000	0.01737	-208.53	-0.4745	0.0001380	-120
-115	0.000103	8.664	0.000	8.664	-7.588	0.000	-7.588	0.03110	0.00000	0.03110	-206.78	-0.4665	0.0001430	-115
-110	0.000102	8.792	0.000	8.792	-6.354	0.000	-6.354	0.04483	0.00000	0.04483	-205.03	-0.4580	0.0001480	-110
-105	0.000101	8.919	0.000	8.919	-5.120	0.000	-5.120	0.05856	0.00000	0.05856	-203.28	-0.4495	0.0001530	-105
-100	0.000100	9.046	0.000	9.046	-3.886	0.001	-3.886	0.07229	0.00000	0.07229	-201.53	-0.4410	0.0001580	-100
-95	0.000099	9.173	0.000	9.173	-2.652	0.002	-2.652	0.08602	0.00000	0.08602	-199.78	-0.4325	0.0001630	-95
-90	0.000098	9.300	0.000	9.300	-1.418	0.002	-1.418	0.10000	0.00001	0.10000	-198.03	-0.4240	0.0001680	-90
-85	0.000097	9.427	0.000	9.427	-0.184	0.003	-0.184	0.11400	0.00001	0.11400	-196.28	-0.4155	0.0001730	-85
-80	0.000096	9.554	0.000	9.554	0.050	0.003	0.050	0.12800	0.00001	0.12800	-194.53	-0.4070	0.0001780	-80
-75	0.000095	9.681	0.000	9.681	1.284	0.003	1.284	0.14200	0.00002	0.14200	-192.78	-0.3985	0.0001830	-75
-70	0.000094	9.808	0.000	9.808	2.518	0.003	2.518	0.15600	0.00003	0.15600	-191.03	-0.3900	0.0001880	-70
-65	0.000093	9.935	0.000	9.935	3.752	0.003	3.752	0.17000	0.00003	0.17000	-189.28	-0.3815	0.0001930	-65
-60	0.000092	10.062	0.000	10.062	4.986	0.003	4.986	0.18400	0.00004	0.18400	-187.53	-0.3730	0.0001980	-60
-55	0.000091	10.189	0.000	10.189	6.220	0.003	6.220	0.19800	0.00004	0.19800	-185.78	-0.3645	0.0002030	-55
-50	0.000090	10.316	0.000	10.316	7.454	0.003	7.454	0.21200	0.00005	0.21200	-184.03	-0.3560	0.0002080	-50
-45	0.000089	10.443	0.001	10.443	8.688	0.004	8.688	0.22600	0.00005	0.22600	-182.28	-0.3475	0.0002130	-45
-40	0.000088	10.570	0.001	10.570	9.922	0.004	9.922	0.24000	0.00006	0.24000	-180.53	-0.3390	0.0002180	-40
-35	0.000087	10.697	0.001	10.697	11.156	0.004	11.156	0.25400	0.00006	0.25400	-178.78	-0.3305	0.0002230	-35
-30	0.000086	10.824	0.001	10.824	12.390	0.004	12.390	0.26800	0.00007	0.26800	-177.03	-0.3220	0.0002280	-30
-25	0.000085	10.951	0.001	10.951	13.624	0.004	13.624	0.28200	0.00007	0.28200	-175.28	-0.3135	0.0002330	-25
-20	0.000084	11.078	0.001	11.078	14.858	0.004	14.858	0.29600	0.00008	0.29600	-173.53	-0.3050	0.0002380	-20
-15	0.000083	11.205	0.001	11.205	16.092	0.004	16.092	0.31000	0.00008	0.31000	-171.78	-0.2965	0.0002430	-15
-10	0.000082	11.332	0.001	11.332	17.326	0.004	17.326	0.32400	0.00009	0.32400	-170.03	-0.2880	0.0002480	-10
-5	0.000081	11.459	0.001	11.459	18.560	0.004	18.560	0.33800	0.00009	0.33800	-168.28	-0.2795	0.0002530	-5
0	0.000080	11.586	0.001	11.586	19.794	0.004	19.794	0.35200	0.00010	0.35200	-166.53	-0.2710	0.0002580	0
5	0.000079	11.713	0.001	11.713	21.028	0.004	21.028	0.36600	0.00010	0.36600	-164.78	-0.2625	0.0002630	5
10	0.000078	11.840	0.001	11.840	22.262	0.004	22.262	0.38000	0.00011	0.38000	-163.03	-0.2540	0.0002680	10
15	0.000077	11.967	0.001	11.967	23.496	0.004	23.496	0.39400	0.00011	0.39400	-161.28	-0.2455	0.0002730	15
20	0.000076	12.094	0.001	12.094	24.730	0.004	24.730	0.40800	0.00012	0.40800	-159.53	-0.2370	0.0002780	20
25	0.000075	12.221	0.001	12.221	25.964	0.004	25.964	0.42200	0.00012	0.42200	-157.78	-0.2285	0.0002830	25
30	0.000074	12.348	0.001	12.348	27.198	0.004	27.198	0.43600	0.00013	0.43600	-156.03	-0.2200	0.0002880	30
35	0.000073	12.475	0.001	12.475	28.432	0.004	28.432	0.45000	0.00013	0.45000	-154.28	-0.2115	0.0002930	35
40	0.000072	12.602	0.001	12.602	29.666	0.004	29.666	0.46400	0.00014	0.46400	-152.53	-0.2030	0.0002980	40
45	0.000071	12.729	0.001	12.729	30.900	0.004	30.900	0.47800	0.00014	0.47800	-150.78	-0.1945	0.0003030	45
50	0.000070	12.856	0.001	12.856	32.134	0.004	32.134	0.49200	0.00015	0.49200	-149.03	-0.1860	0.0003080	50
55	0.000069	12.983	0.001	12.983	33.368	0.004	33.368	0.50600	0.00015	0.50600	-147.28	-0.1775	0.0003130	55
60	0.000068	13.110	0.001	13.110	34.602	0.004	34.602	0.52000	0.00016	0.52000	-145.53	-0.1690	0.0003180	60
65	0.000067	13.237	0.001	13.237	35.836	0.004	35.836	0.53400	0.00016	0.53400	-143.78	-0.1605	0.0003230	65
70	0.000066	13.364	0.001	13.364	37.070	0.004	37.070	0.54800	0.00017	0.54800	-142.03	-0.1520	0.0003280	70
75	0.000065	13.491	0.001	13.491	38.304	0.004	38.304	0.56200	0.00017	0.56200	-140.28	-0.1435	0.0003330	75
80	0.000064	13.618	0.001	13.618	39.538	0.004	39.538	0.57600	0.00018	0.57600	-138.53	-0.1350	0.0003380	80
85	0.000063	13.745	0.001	13.745	40.772	0.004	40.772	0.59000	0.00018	0.59000	-136.78	-0.1265	0.0003430	85
90	0.000062	13.872	0.001	13.872	42.006	0.004	42.006	0.60400	0.00019	0.60400	-135.03	-0.1180	0.0003480	90
95	0.000061	14.000	0.001	14.000	43.240	0.004	43.240	0.61800	0.00019	0.61800	-133.28	-0.1095	0.0003530	95
100	0.000060	14.127	0.001	14.127	44.474	0.004	44.474	0.63200	0.00020	0.63200	-131.53	-0.1010	0.0003580	100
105	0.000059	14.254	0.001	14.254	45.708	0.004	45.708	0.64600	0.00020	0.64600	-129.78	-0.0925	0.0003630	105
110	0.000058	14.381	0.001	14.381	46.942	0.004	46.942	0.66000	0.00021	0.66000	-128.03	-0.0840	0.0003680	110
115	0.000057	14.508	0.001	14.508	48.176	0.004	48.176	0.67400	0.00021	0.67400	-126.28	-0.0755	0.0003730	115
120	0.000056	14.635	0.001	14.635	49.410	0.004	49.410	0.68800	0.00022	0.68800	-124.53	-0.0670	0.0003780	120
125	0.000055	14.762	0.001	14.762	50.644	0.004	50.644	0.70200	0.00022	0.70200	-122.78	-0.0585	0.0003830	125
130	0.000054	14.889	0.001	14.889	51.878	0.004	51.878	0.71600	0.00023	0.71600	-121.03	-0.0500	0.0003880	130
135	0.000053	15.016	0.001	15.016	53.112	0.004	53.112	0.73000	0.00023	0.73000	-119.28	-0.0415	0.0003930	135
140	0.000052	15.143	0.001	15.143	54.346	0.004	54.346	0.74400	0.00024	0.74400	-117.53	-0.0330	0.0003980	140
145	0.000051	15.270	0.001	15.270	55.580	0.004	55.580	0.75800	0.00024	0.75800	-115.78	-0.0245	0.0004030	145
150	0.000050	15.397	0.001	15.397	56.814	0.004	56.814	0.77200	0.00025	0.77200	-114.03	-0.0160	0.0004080	150
155	0.000049	15.524	0.001	15.524	58.048	0.004	58.048	0.78600	0.00025	0.78600	-112.28	-0.0075	0.0004130	155
160	0.000048	15.651	0.001	15.651	59.282	0.004	59.282	0.80000	0.00026	0.80000	-110.53	0.0010	0.0004180	160